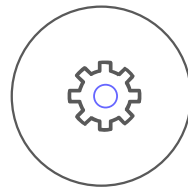


Chapter 1 Zero resistance



Introduction



Experimental Methods



Summary



Introduction



Through measurement to knowledge.

H. Kamerlingh Onnes

1908年，成功制备液氦[沸点4.2 K];

1911年，发现超导现象;

1913年，获得诺贝尔物理学奖.

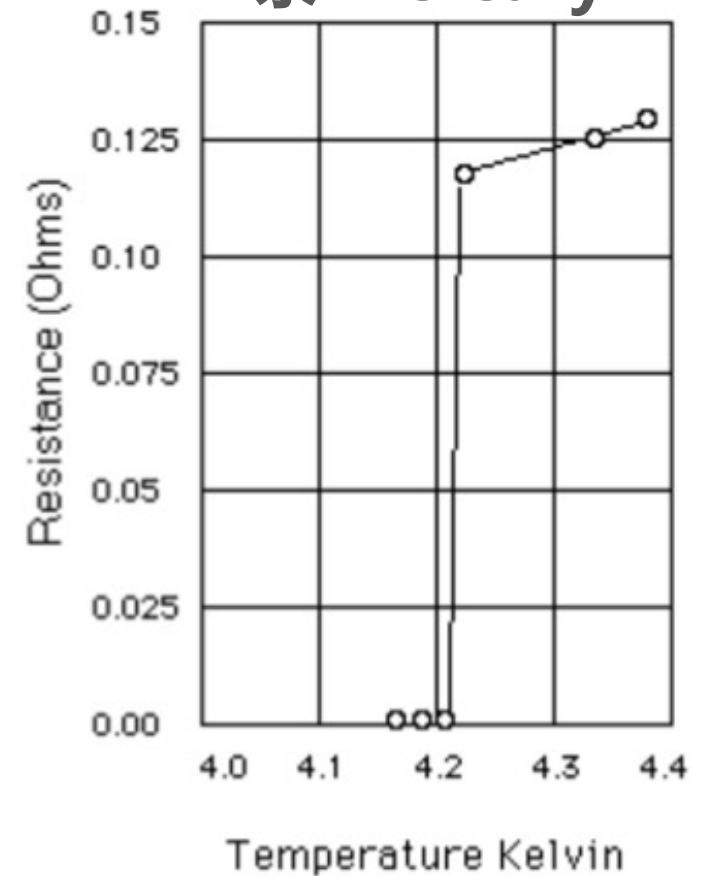
热力学温度

$$T(\text{K}) = T(^{\circ}\text{C}) + 273.15$$

$$4.2 \text{ K} = -268.95 ^{\circ}\text{C}$$

很cool的现象

汞 Mercury

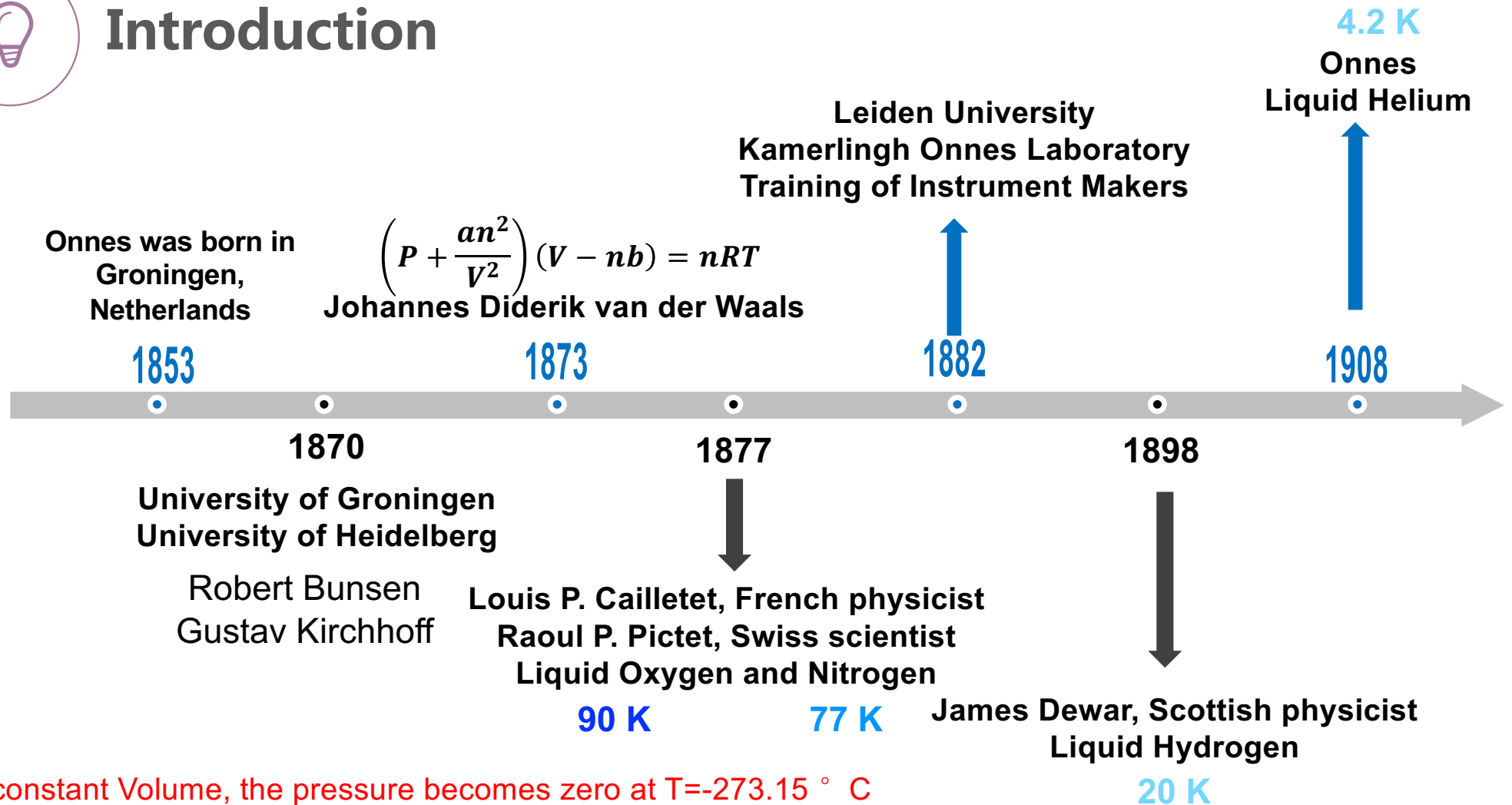


H. K. Onnes, Commun. Phys. Lab. 12, 120 (1911).

Discovery of superconductivity



Introduction

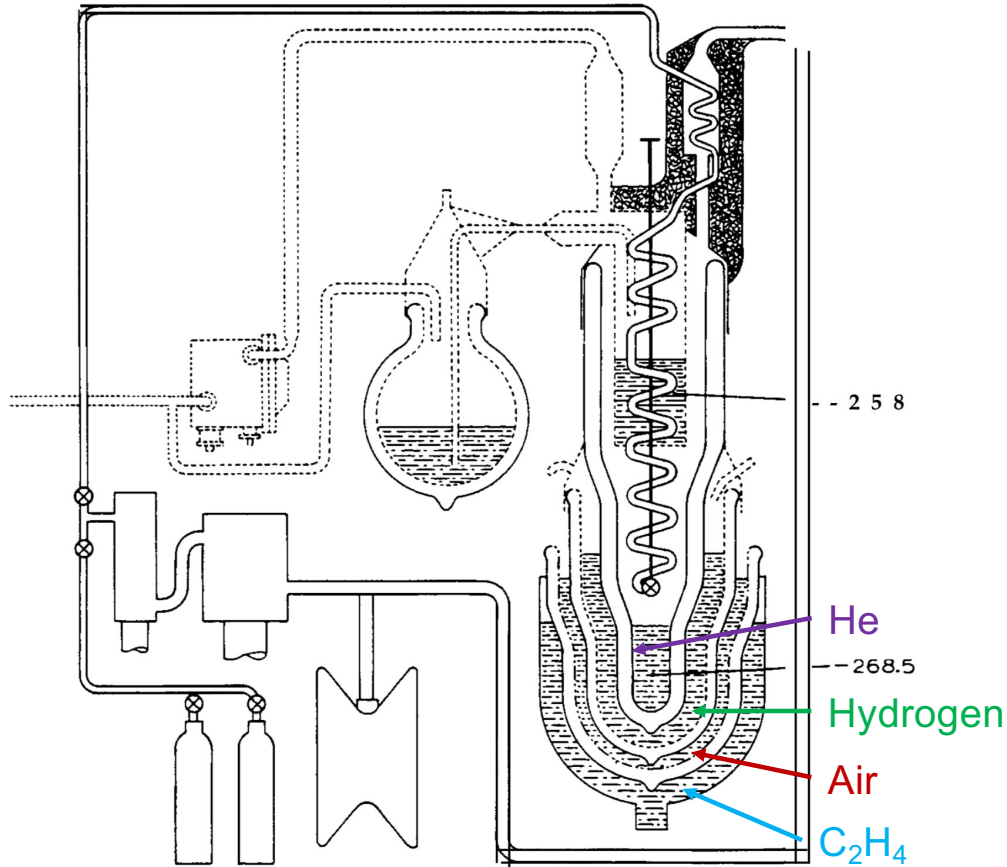


At constant Volume, the pressure becomes zero at $T = -273.15^\circ \text{C}$

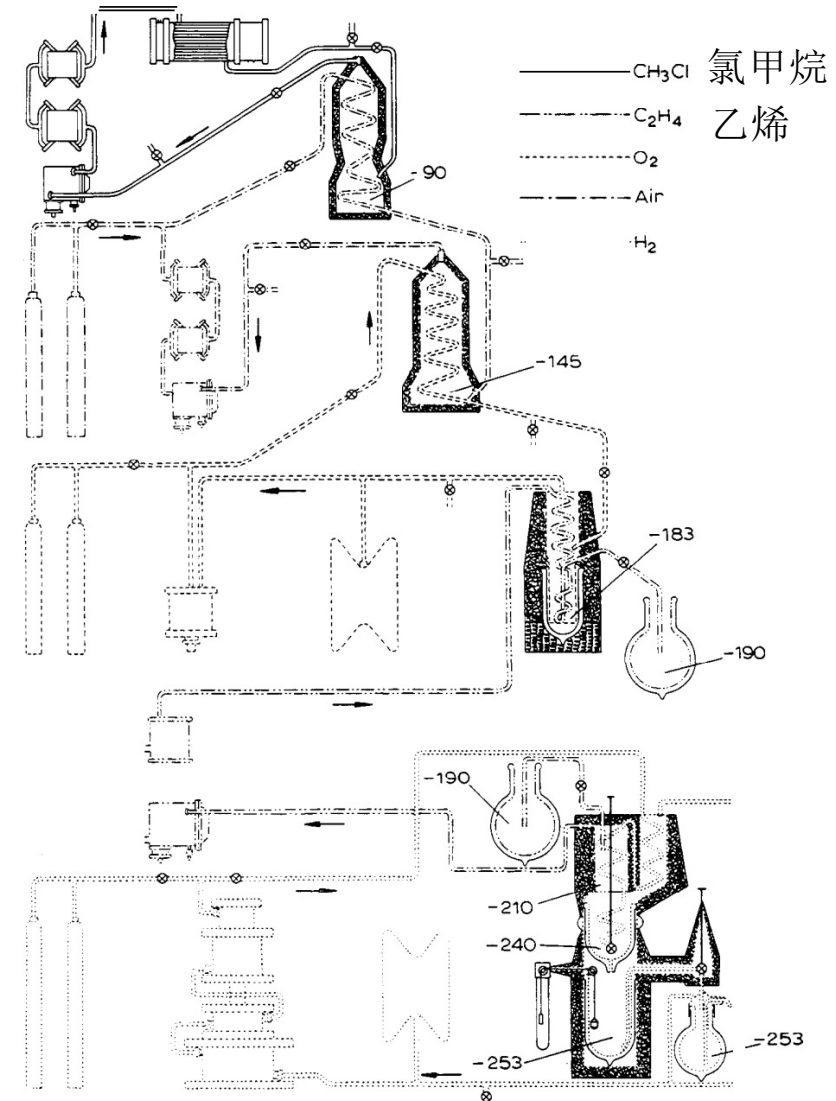
Discovery of superconductivity



Introduction



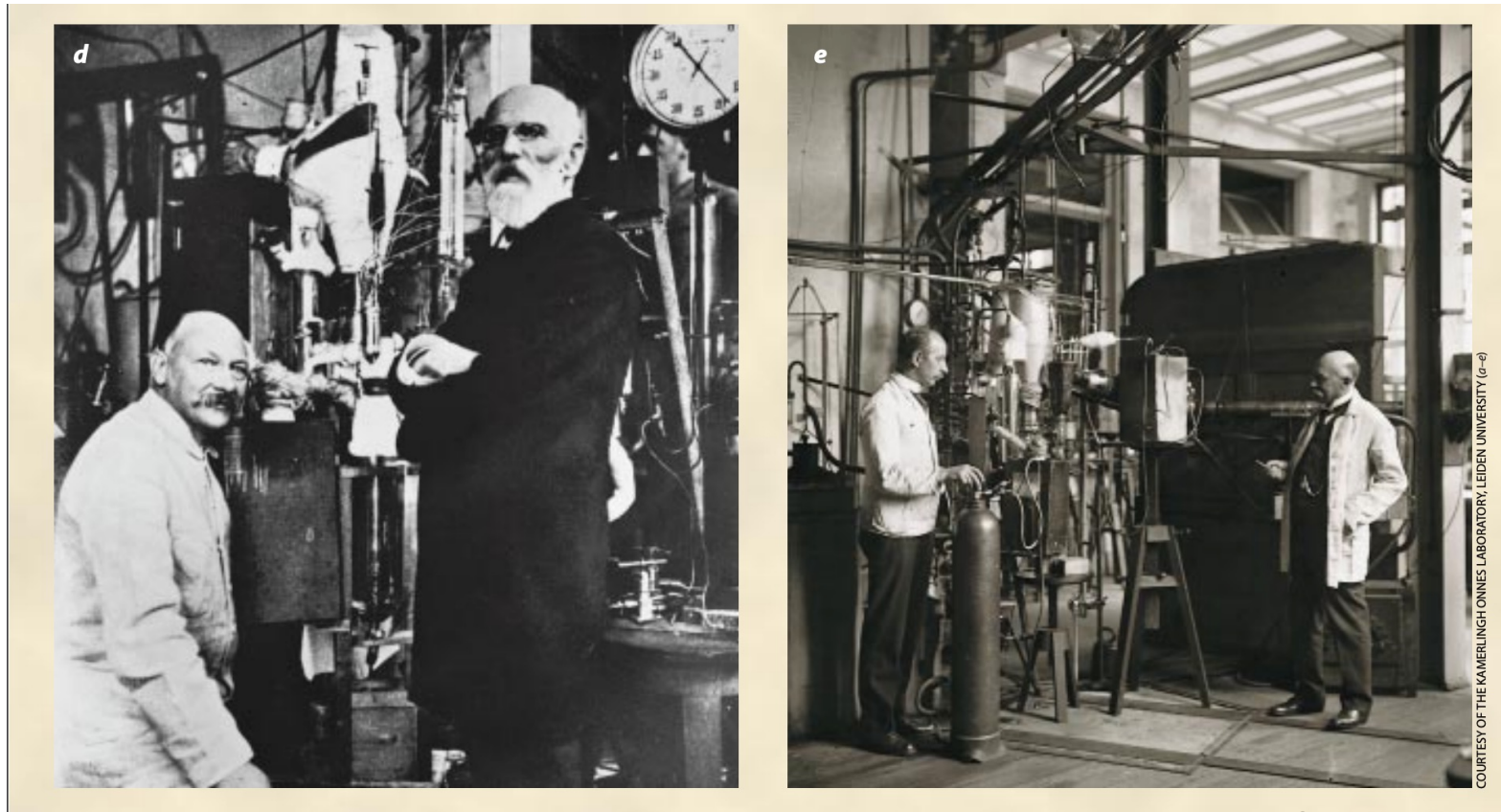
Onnes Nobel Lecture, December 11, 1913



Discovery of superconductivity



Introduction



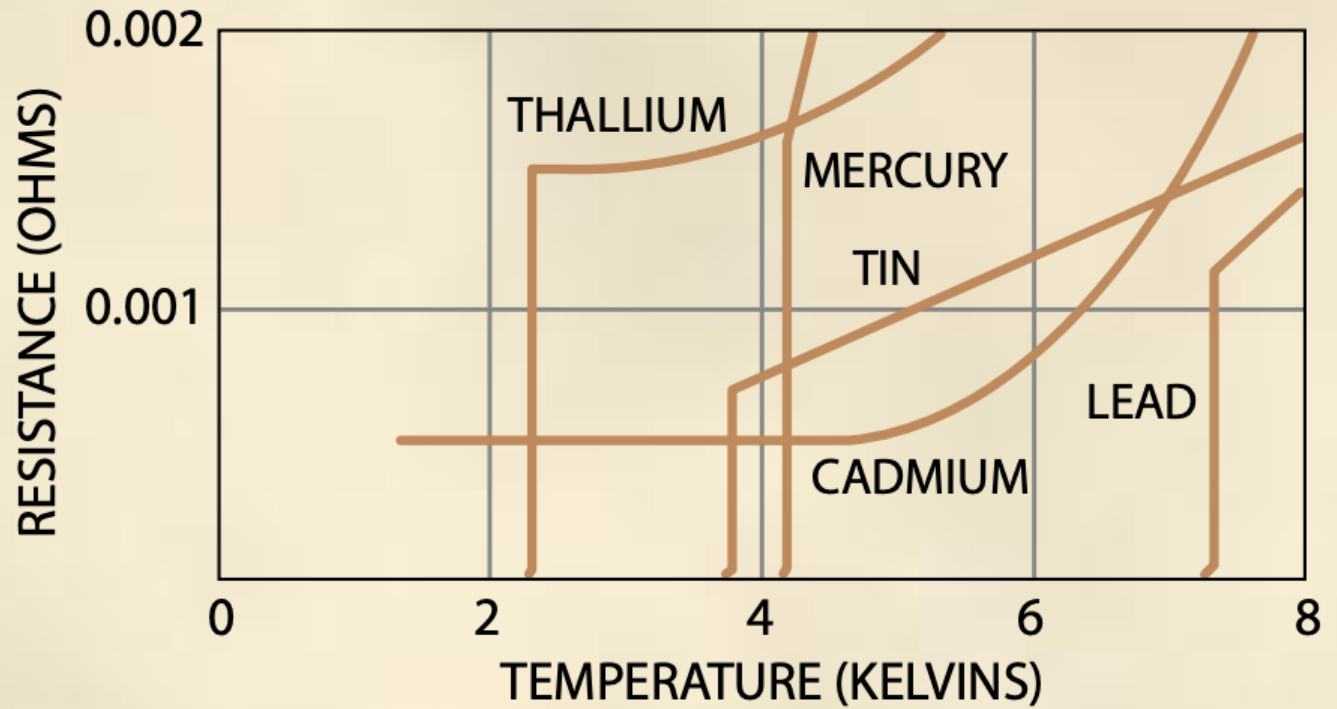
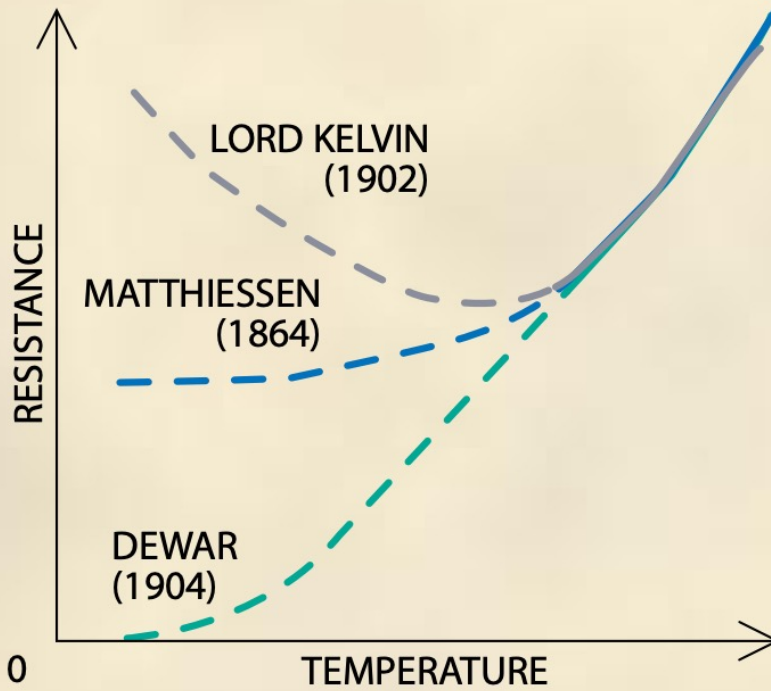
Onnes **van der Waals**
1911

Gerrit Flim **Onnes**
Rudolf de Bruyn Ouboter Scientific American 1997

Discovery of superconductivity



Introduction



Rudolf de Bruyn Ouboter Scientific American 1997

Discovery of superconductivity



Introduction

Superconducting Elements

																		P = 1 bar (29)																
																		P > 1 bar (16)																
																		we found (7)																
¹ H																			² He															
³ Li	⁴ Be															⁵ B	⁶ C	⁷ N	⁸ O	⁹ F	¹⁰ Ne													
¹¹ Na	¹² Mg															¹³ Al	¹⁴ Si	¹⁵ P	¹⁶ S	¹⁷ Cl	¹⁸ Ar													
¹⁹ K	²⁰ Ca	²¹ Sc	²² Ti	²³ V	²⁴ Cr	²⁵ Mn	²⁶ Fe	²⁷ Co	²⁸ Ni	²⁹ Cu	³⁰ Zn	³¹ Ga	³² Ge	³³ As	³⁴ Se	³⁵ Br	³⁶ Kr																	
³⁷ Rb	³⁸ Sr	³⁹ Y	⁴⁰ Zr	⁴¹ Nb	⁴² Mo	⁴³ Tc	⁴⁴ Ru	⁴⁵ Rh	⁴⁶ Pd	⁴⁷ Ag	⁴⁸ Cd	⁴⁹ In	⁵⁰ Sn	⁵¹ Sb	⁵² Te	⁵³ I	⁵⁴ Xe																	
⁵⁵ Cs	⁵⁶ Ba	⁵⁷ La	⁷² Hf	⁷³ Ta	⁷⁴ W	⁷⁵ Re	⁷⁶ Os	⁷⁷ Ir	⁷⁸ Pt	⁷⁹ Au	⁸⁰ Hg	⁸¹ Tl	⁸² Pb	⁸³ Bi	⁸⁴ Po	⁸⁵ At	⁸⁶ Rn																	
⁸⁷ Fr	⁸⁸ Ra	⁸⁹ Ac																																
																		⁵⁸ Ce	⁵⁹ Pr	⁶⁰ Nd	⁶¹ Pm	⁶² Sm	⁶³ Eu	⁶⁴ Gd	⁶⁵ Tb	⁶⁶ Dy	⁶⁷ Ho	⁶⁸ Er	⁶⁹ Tm	⁷⁰ Yb	⁷¹ Lu			
																		⁹⁰ Th	⁹¹ Pa	⁹² U	⁹³ Np	⁹⁴ Pu	⁹⁵ Am	⁹⁶ Cm	⁹⁷ Bk	⁹⁸ Cf	⁹⁹ Es	¹⁰⁰ Fm	¹⁰¹ Md	¹⁰² No	¹⁰³ Lr			

Figure 1. Superconducting elements in the periodic table. The elements paint in pink are superconductor under normal condition ($P = 0$ bar); 29 elements. The ones in red are superconductors under pressure ($P > 1$ bar); 23 elements, in which author group has found 7 elements.

Superconducting Elements



Introduction

Blue boy story?

An apprentice from the instrument-maker's school Kamerlingh Onnes had founded. (The appellation refers to the blue uniforms the boys wore.) As the story goes, the blue boy's sleepy inattention that afternoon had let the helium boil, thus raising the mercury above its 4.2-K transition temperature and signaling the new state—by its reversion to normal conductivity—with a dramatic swing of the galvanometer.



Discovery of superconductivity



Introduction

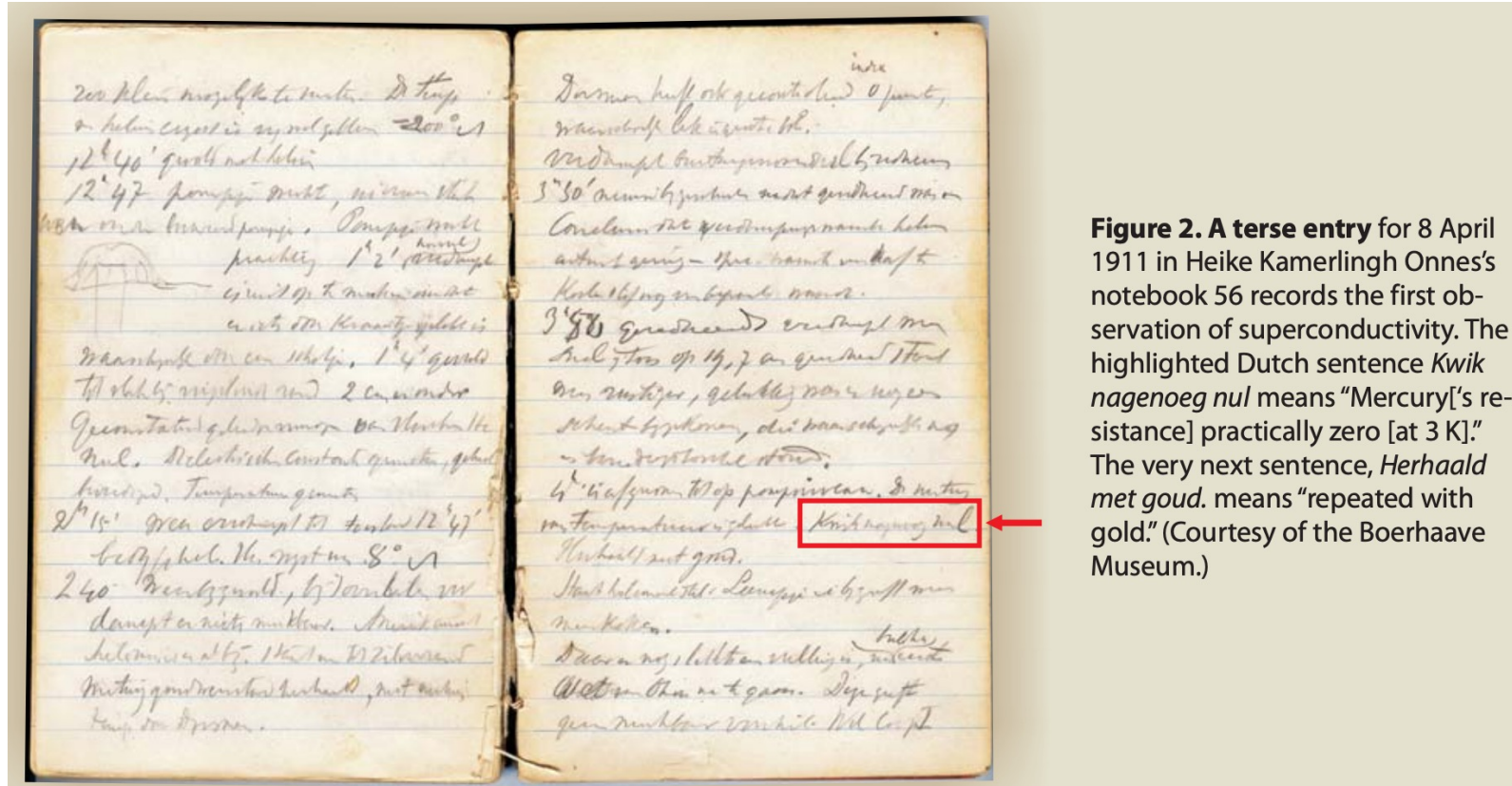


Figure 2. A terse entry for 8 April 1911 in Heike Kamerlingh Onnes's notebook 56 records the first observation of superconductivity. The highlighted Dutch sentence *Kwik nagenoeg nul* means "Mercury[*'s* resistance] practically zero [at 3 K]." The very next sentence, *Herhaald met goud*, means "repeated with gold." (Courtesy of the Boerhaave Museum.)

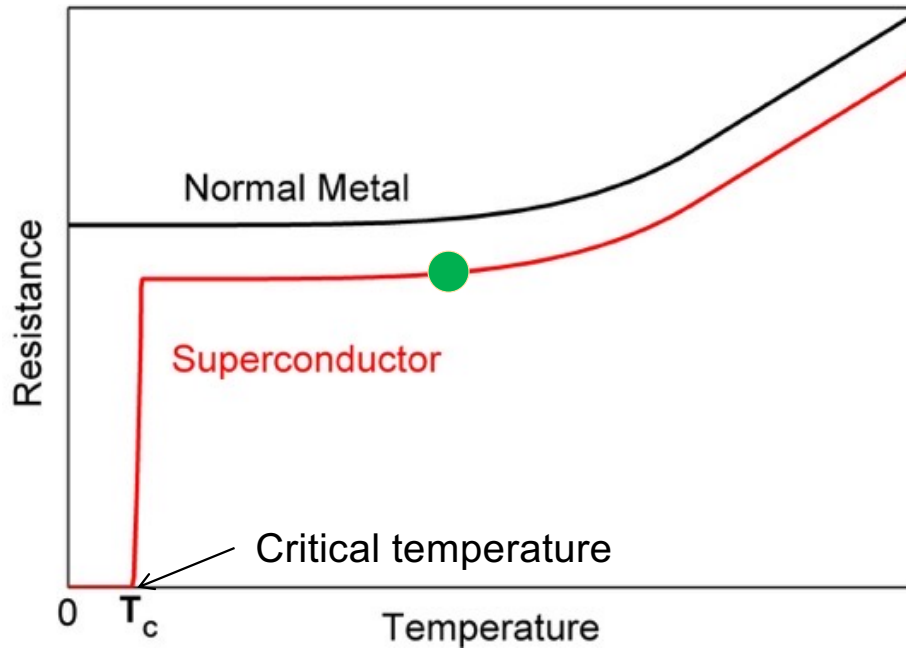


Dirk van Delft and Peter Kes, 2010 *Physics Today*

Discovery of superconductivity



Introduction



Normal Metal

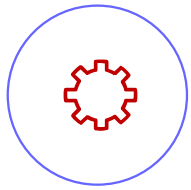


Superconductor

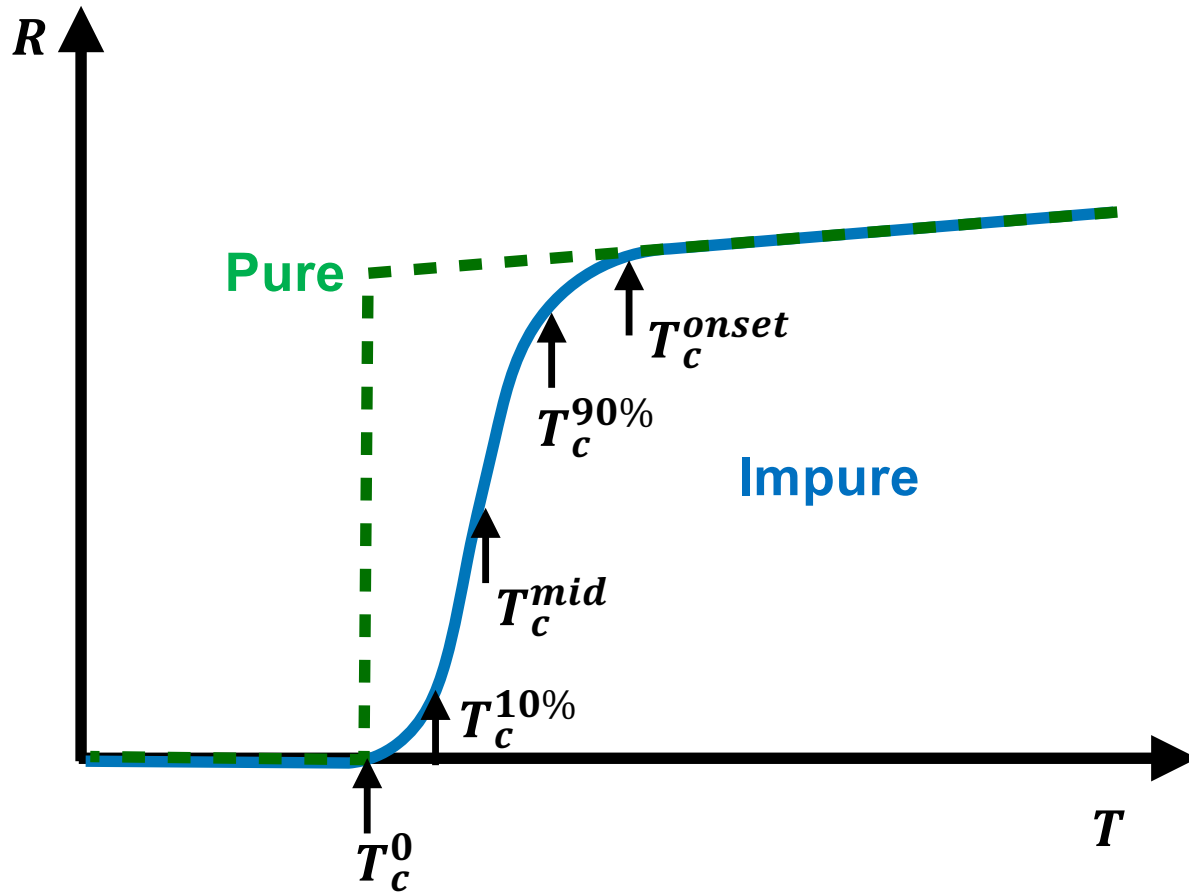


T_c : critical temperature, 临界温度

Zero Resistance and critical temperature



Introduction



How to define T_c ?

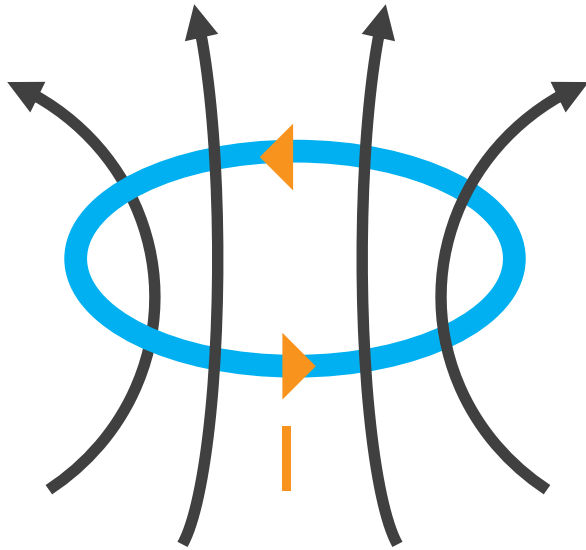
%10、 %50、 %90 R_n

$$\Delta T_c = T_c^{90\%} - T_c^{10\%}$$

Zero Resistance and critical temperature



Introduction



$$\rho < 10^{-26} \Omega m$$

$$\rho_{cu} \sim 10^{-8} \Omega m \text{ at } 300 K$$

$$I(t) = I(0)e^{-t/\tau}$$

$$\tau = L/R$$

L : 电感 (Inductance)

R : 电阻

$$\tau \sim 10^5 \text{ years}$$

or even up to $10^{10^{10}}$ years

Persistent current

Zero Resistance



Introduction

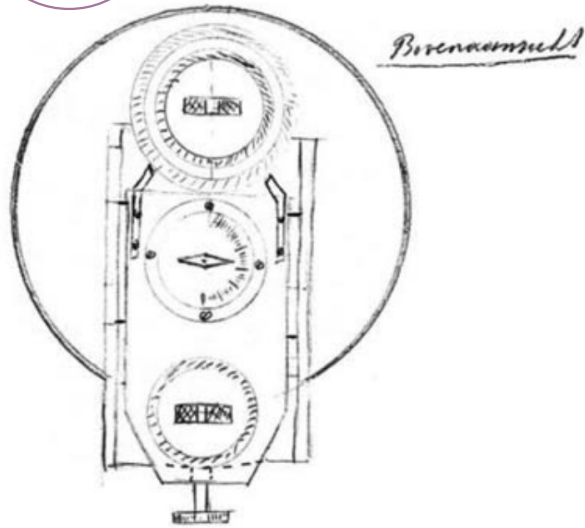


Figure 5. Gerrit Flim's drawing of the setup for a persistent-current experiment in May 1914. In this top view (*bovenaanzicht*), one sees a compass needle pointing north between a superconducting lead coil (west) immersed in liquid helium in a double-walled dewar and a normally conducting copper coil (east) of equal size immersed in liquid air in a single-walled vessel. The copper coil, whose connection to a current source and galvanometer is not shown, calibrates and monitors the persistent current in the superconducting coil. When both currents are equal, the compass points due north. (Courtesy of the Boerhaave Museum.)

Dear Hendrik Lorentz,

I attended a fascinating experiment at the laboratory.... Unsettling, to see the effect of this “permanent” current on a magnetic needle. It is almost palpable, the way the ring of electrons goes round and round and round in the wire, slowly and virtually without friction.

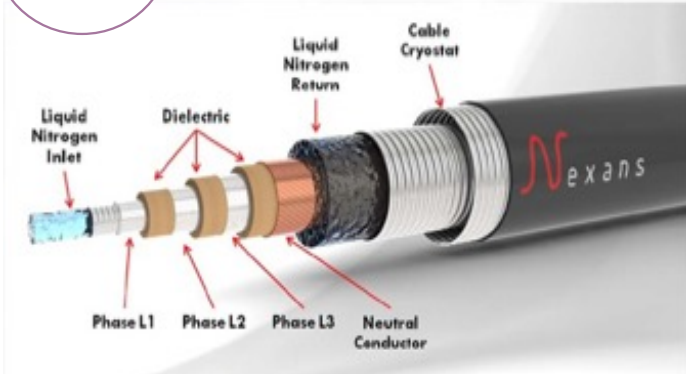
--Paul Ehrenfest

Dirk van Delft and Peter Kes, 2010 *Physics Today*

Zero Resistance



Introduction



Superconducting cables

核磁共振成像仪 MRI



大型强子对撞机

~10 000 个超导磁体
>27 吨



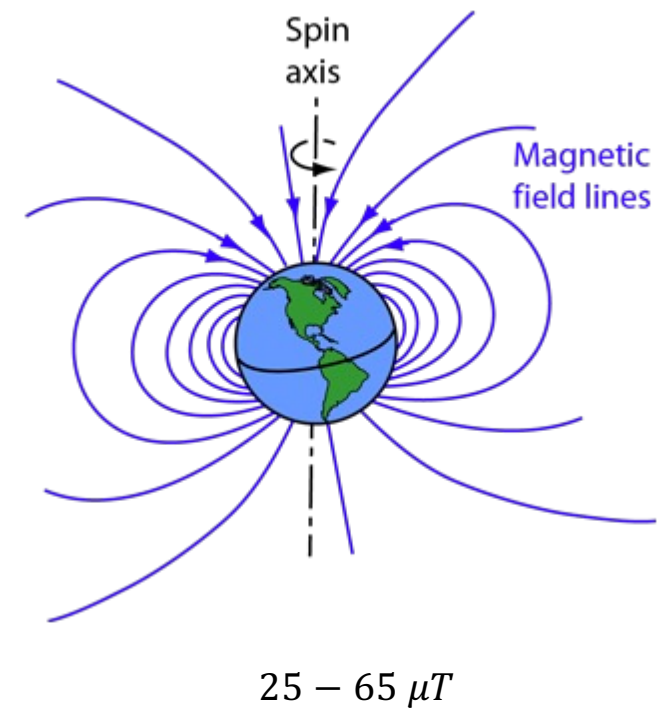
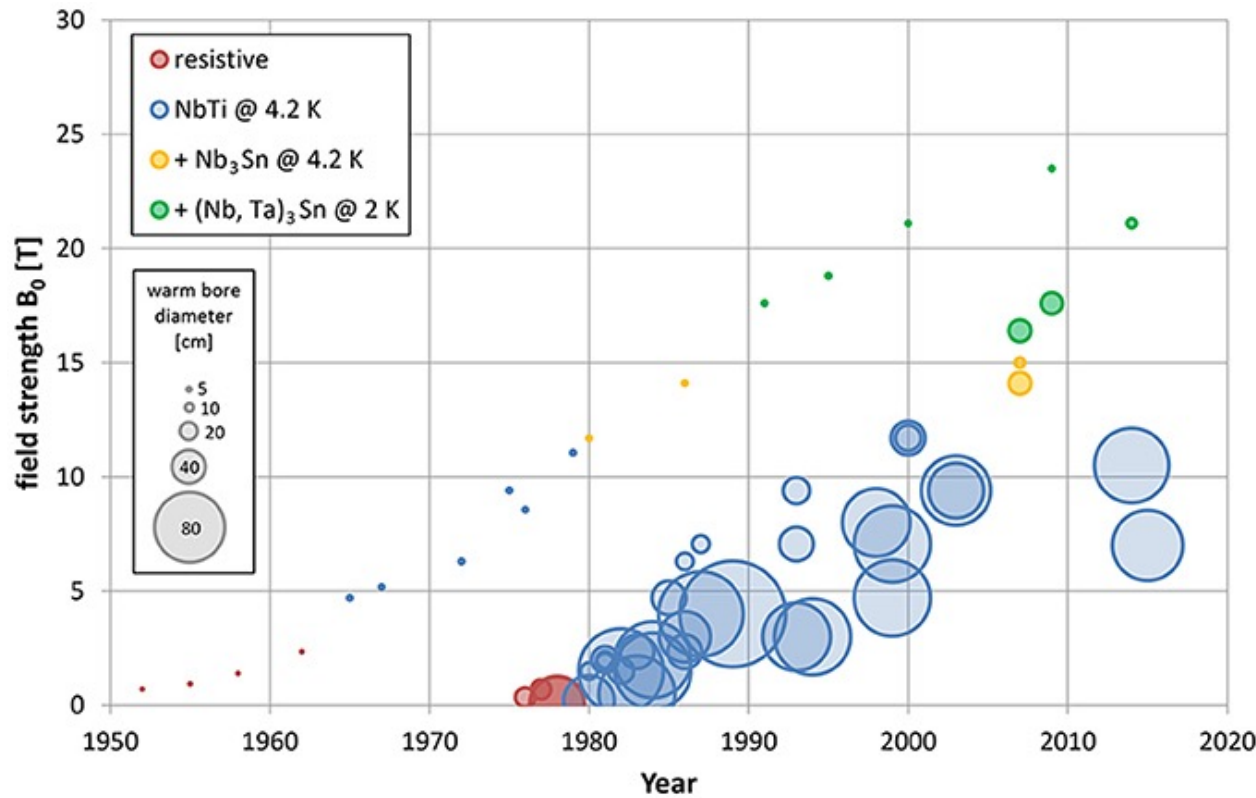
Superconducting Magnet

Applications-zero resistance



Introduction

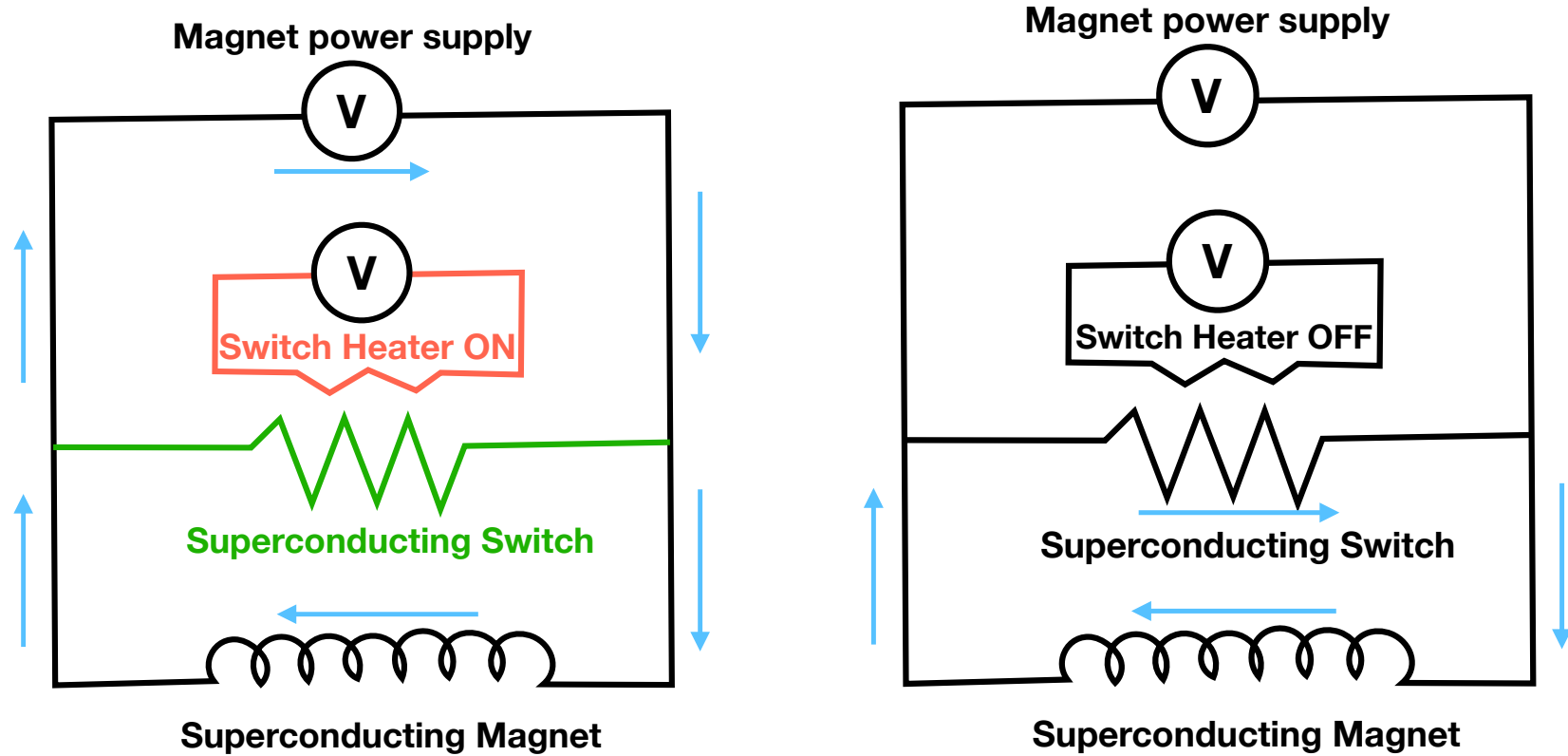
Superconducting Magnet



Applications-zero resistance



Introduction

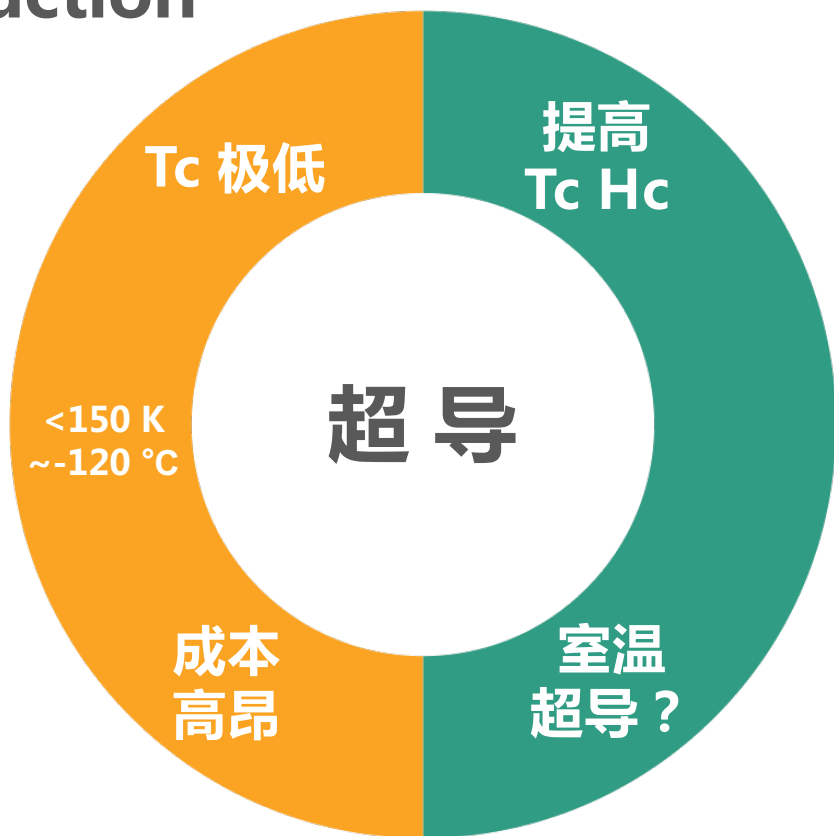


How to drive a Superconducting Magnet into persistent mode?

Applications-zero resistance



Introduction

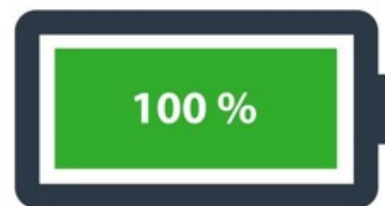


太cool而
不可及

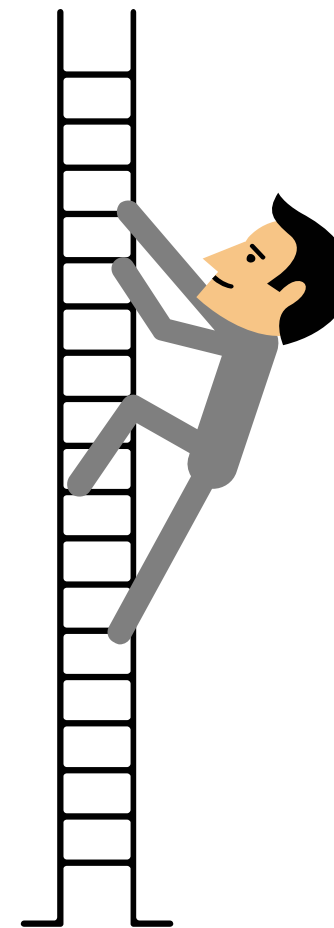
局限

目标

妈妈再也不用担心
我手机没电了!



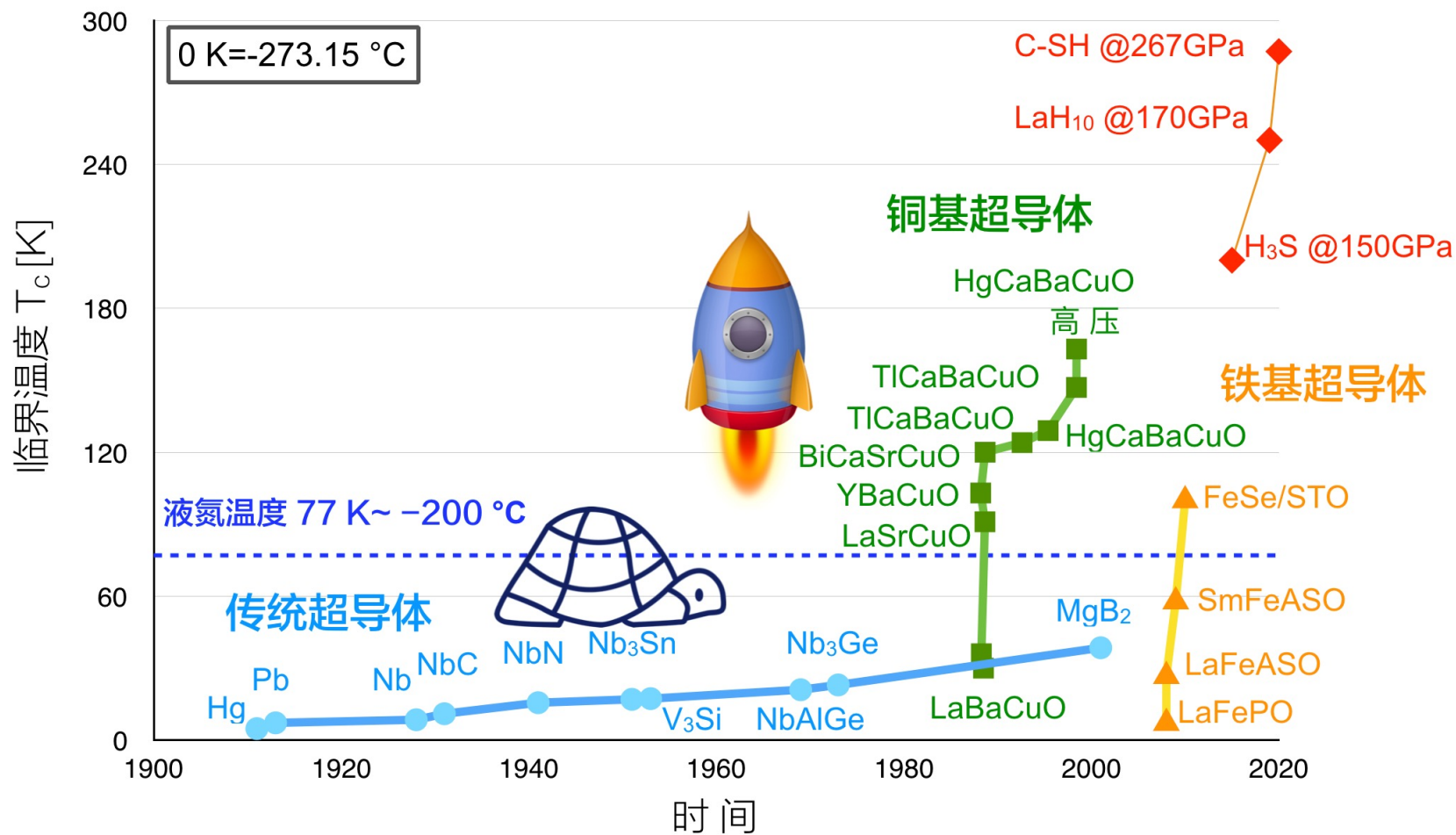
Always 100%!



Limitations



Introduction



100 years in superconductivity



Introduction

Rules of B. Matthias for discovering new superconductors

1. high symmetry is best
2. peaks in density of states are good
3. stay away from oxygen
4. stay away from magnetism
5. stay away from insulators
6. stay away from theorists



这脸打的 pia pia 响

Interpretation of experimental data on odd numbers

- 1, 3, 5, 7 are all prime numbers.
- **All odd numbers are prime numbers.**
- 9 is not a prime number! Error or unique
- **11 13 are prime numbers.**
- 15 is not a prime number.
- infinitely many odd numbers, but not prime numbers .

From Steve Girvin's lecture (Boulder Summer School 2000) courtesy of Matthew Fisher

100 years in superconductivity



Introduction

Discovery of superconductivity H. Kamerlingh Onnes(1911) in Hg
1913 Nobel prize

Perfect diamagnetism: Meissner and Ochsenfeld(1933)

London equation: F. and H. London(1933)

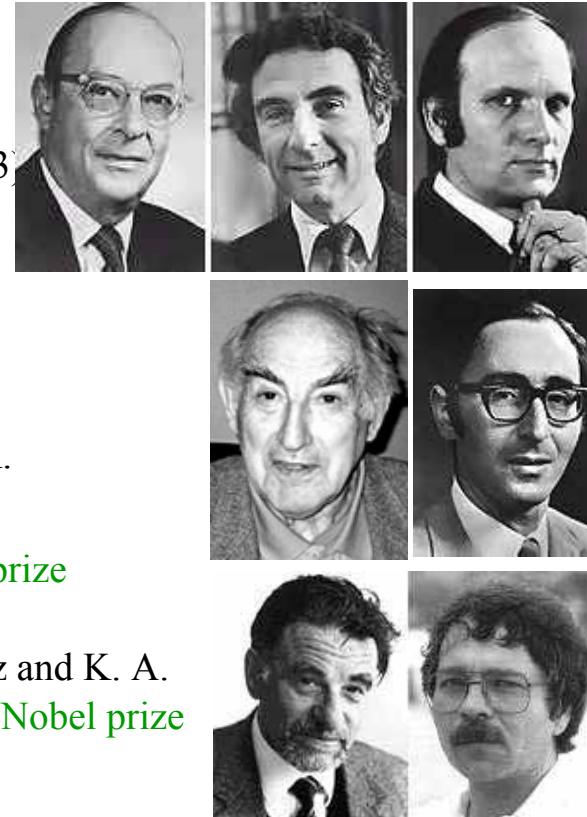
Ginzburg-Landau theory: 1950s
2003 Nobel prize (with Abrikosov)

Isotope effect: H. Frohlich(1950)

BCS theory: J. Bardeen, L. Cooper and J.R. Schrieffer(1957) 1972 Nobel prize

Tunneling: Josephson (1957) 1973 Nobel prize

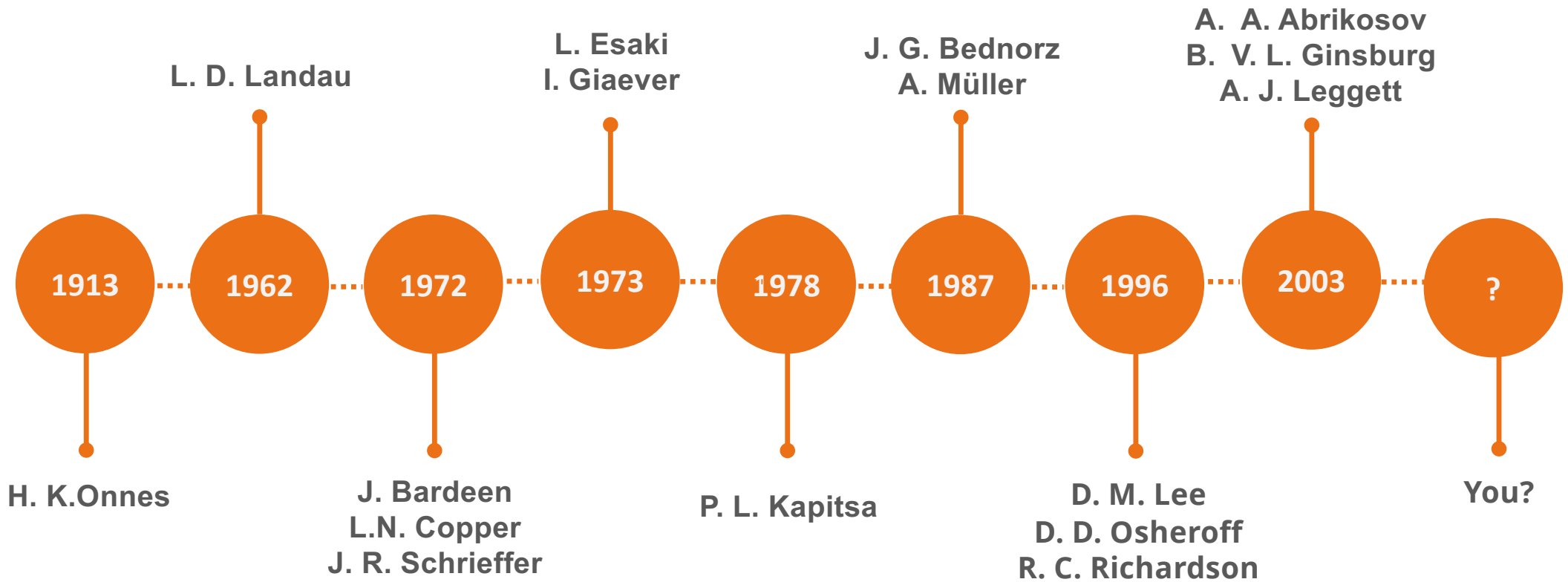
Hi-Tc superconductivity: J. G. Bednorz and K. A. Muller(1986) in Ba-La-Cu-O system. 1987 Nobel prize



100 years in superconductivity



Introduction

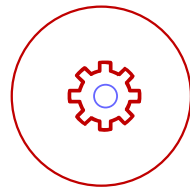


100 years in superconductivity

Chapter 1 Zero resistance



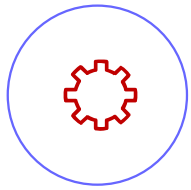
Introduction



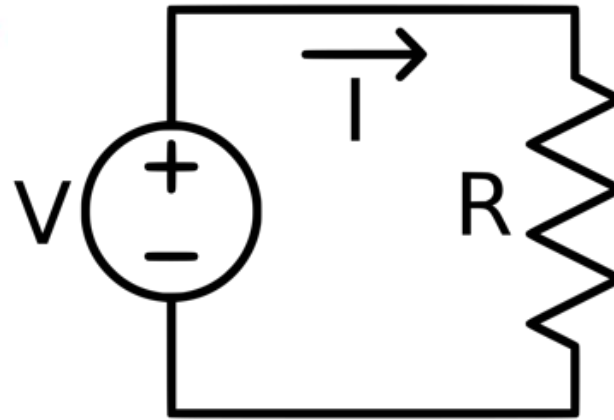
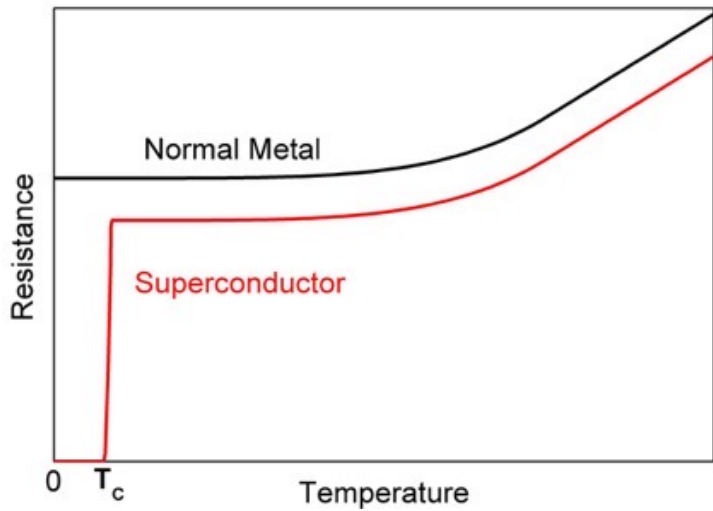
Experimental Methods



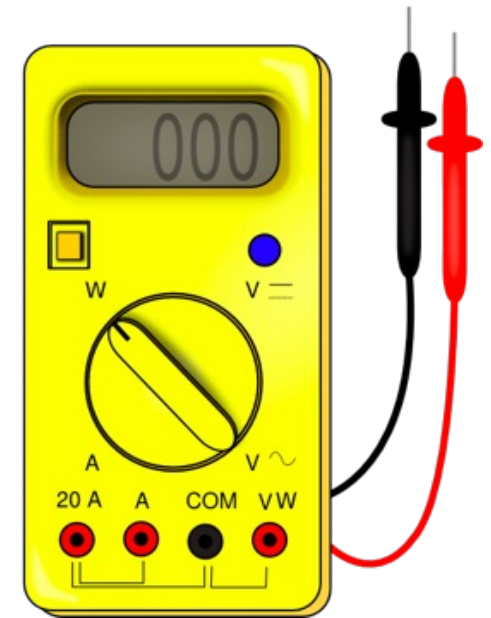
Summary



Experimental Methods

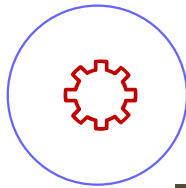


$$R = \frac{V}{I}$$



X

Electrical Transport

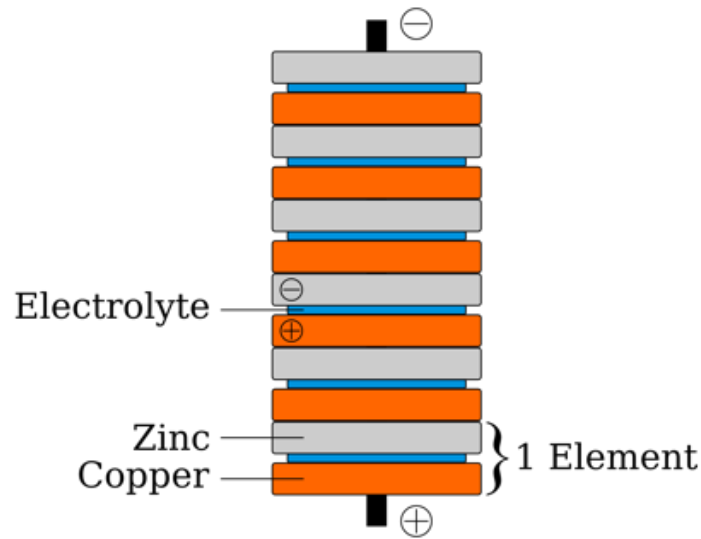


Experimental Methods

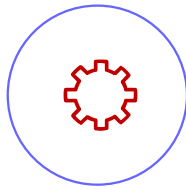


Alessandro Giuseppe Antonio Anastasio Volta
Italian physicist and chemist
1745 – 1827

- Invented electric battery in 1799.
- **Volt** unit adopted internationally in 1881.



Volta explains the principle of the "electric column" to [Napoleon](#) in 1801

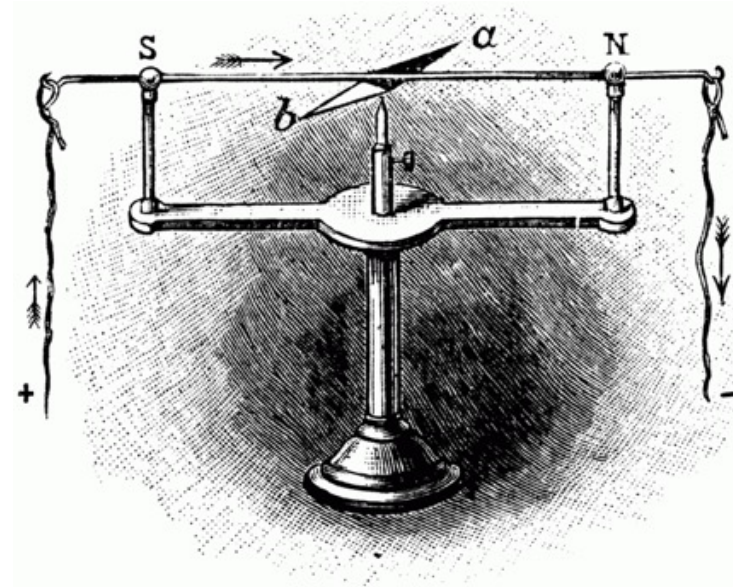


Experimental Methods



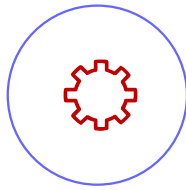
André-Marie Ampère
French physicist and mathematician
1775 – 1836

Father of electrodynamics.



- Months after 1819 Hans Christian Ørsted's discovery of magnetic action of electrical current
- 1820 Law of electromagnetism (Ampère's law) magnetic force between two electric currents.
- First measurement technique for electricity Needle galvanometer .

Electrical Transport



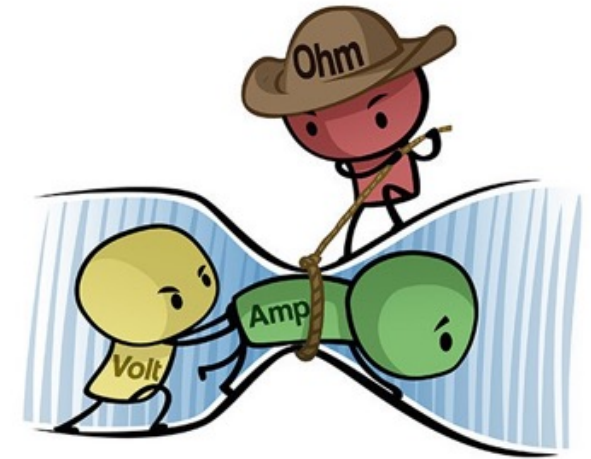
Experimental Methods



Georg Simon Ohm
German physicist and mathematician
1789 –1854

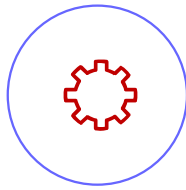


Ohm's law 1827

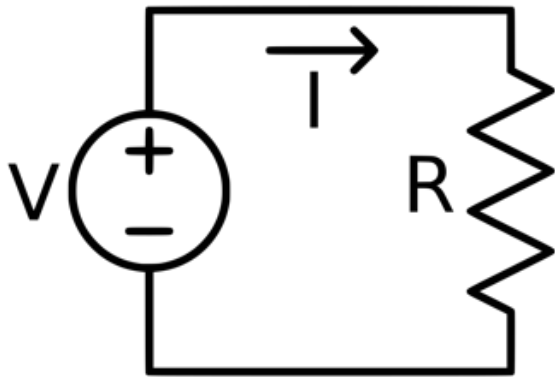


$$I = \frac{V}{R}$$

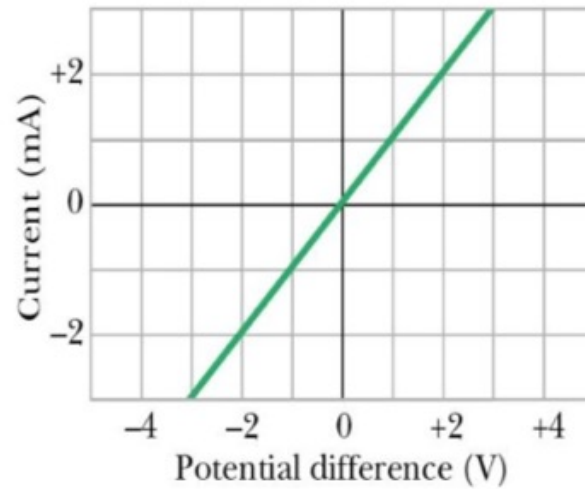
Electrical Transport



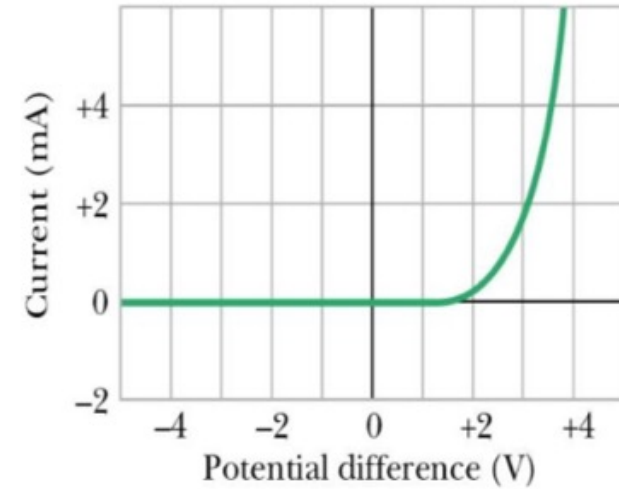
Experimental Methods



那不是小菜一碟



(b)

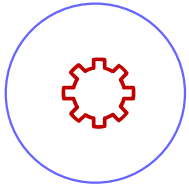


(c)

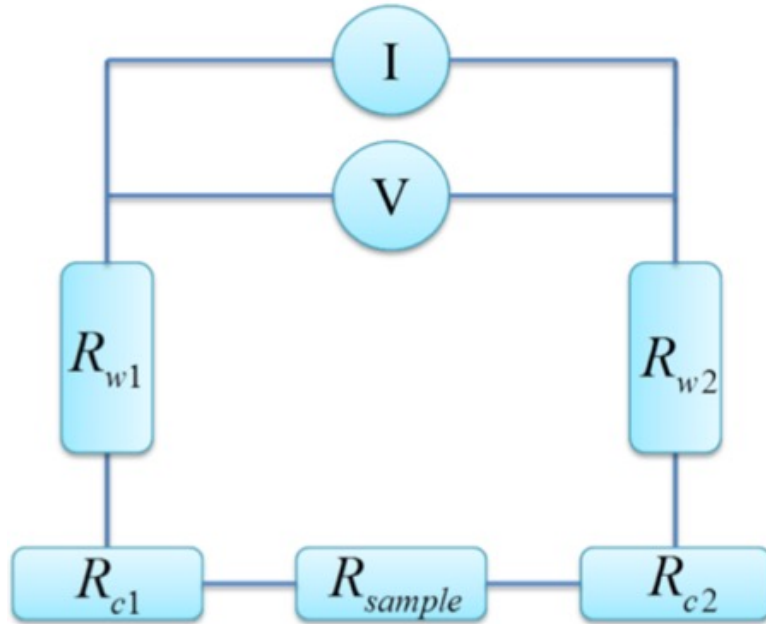
- Ohm's law is valid ONLY when I-V curve is linear!
- Whole circuit is linear and no offsets!
- Wire resistance is negligible!

May be far from true!

Electrical Transport

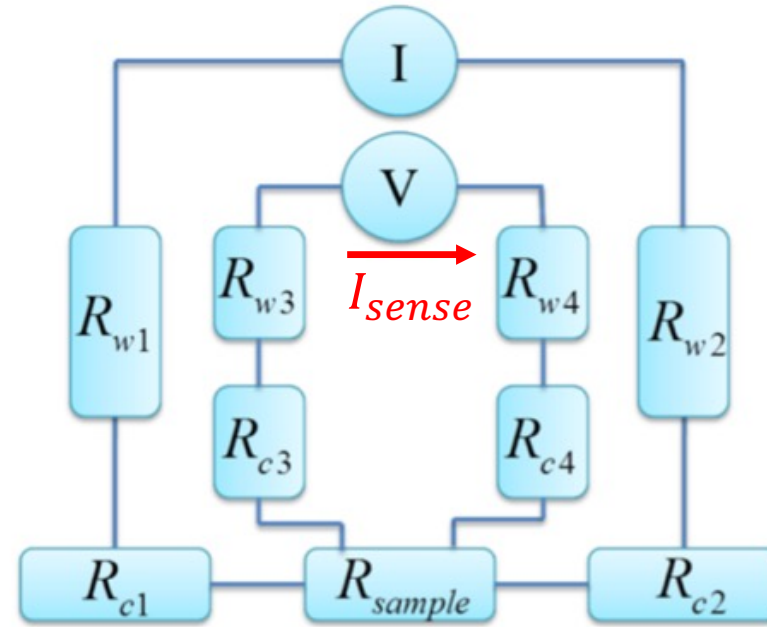


Experimental Methods



2-Probe Method

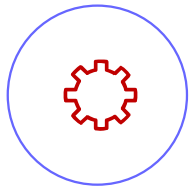
$$R_{Measured} = R_{w1} + R_{w2} + R_{c1} + R_{c2}$$



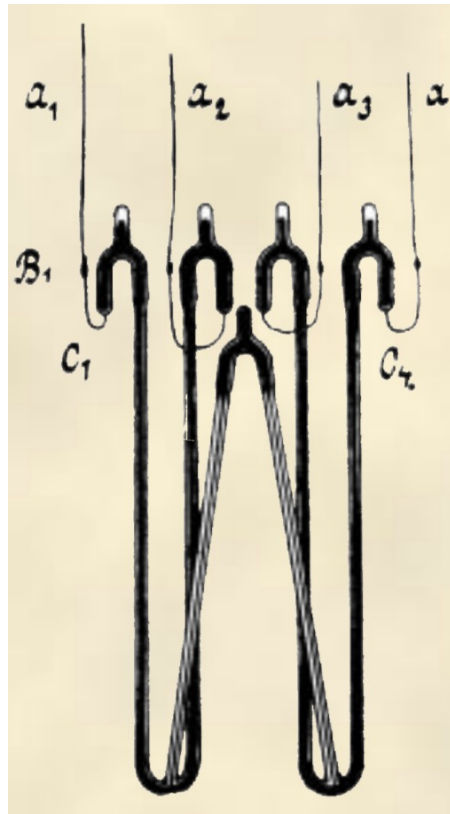
4-Probe Method

$$R_V \gg R_{sample} \quad I_{sense} \text{ is very small}$$

4-Probe Method(Kelvin Method)



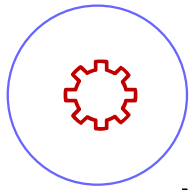
Experimental Methods



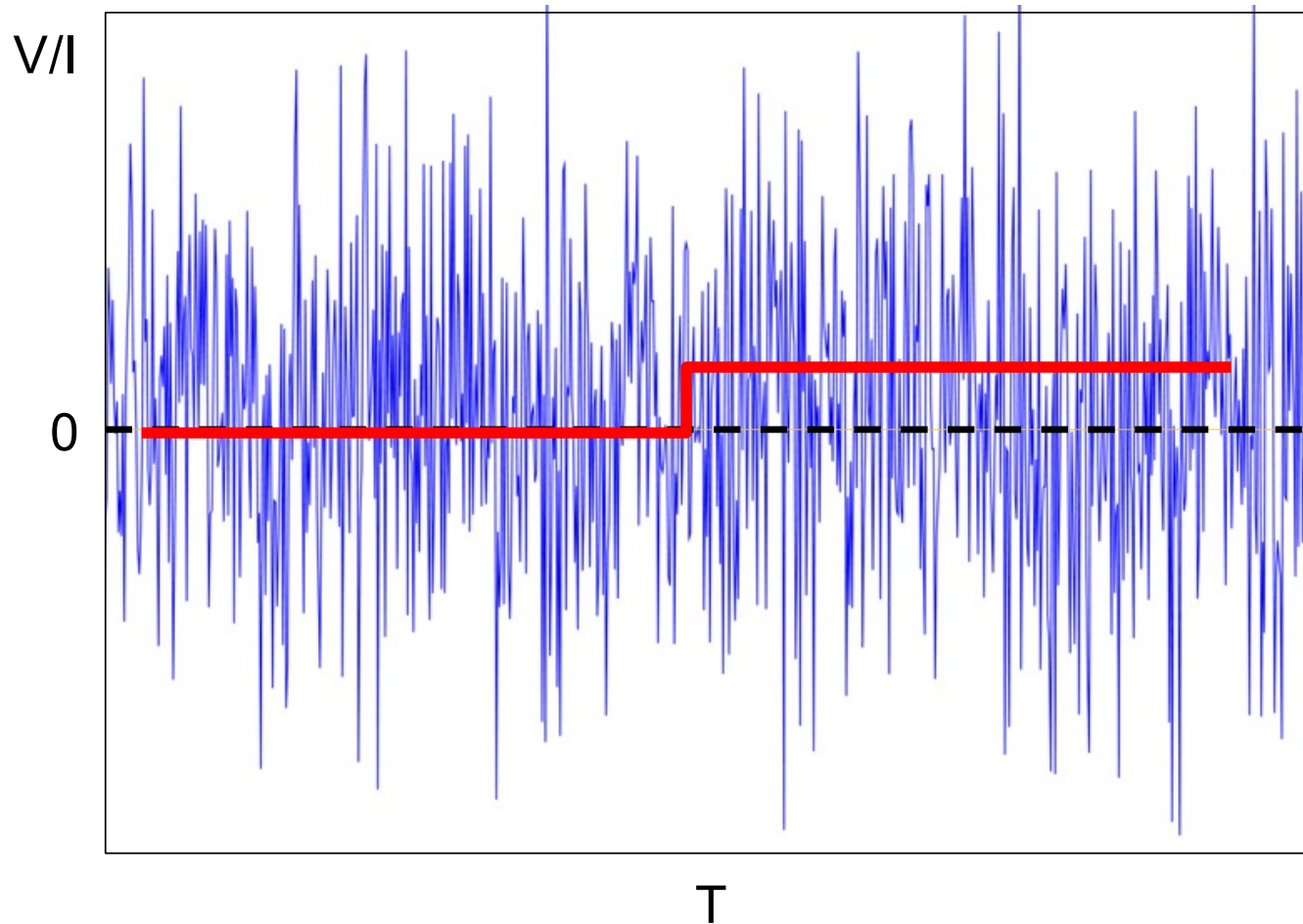
Rudolf de Bruyn Ouboter Scientific American 1997

4-Probe Method (Kelvin Method)

Electrical Transport



Experimental Methods



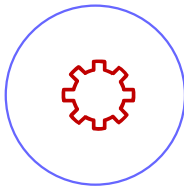
Total signal

Sample signal



我又错过了
几百个亿是吗?

Electrical Transport



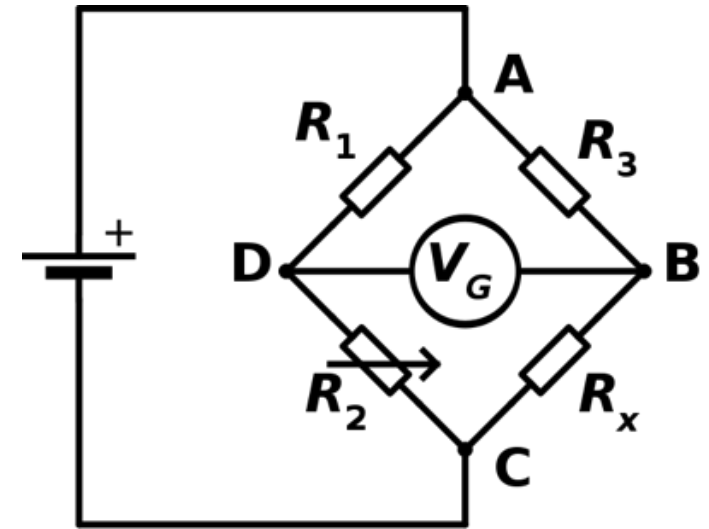
Experimental Methods



Samuel Hunter Christie



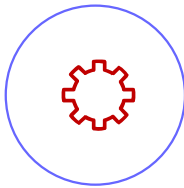
Sir Charles Wheatstone



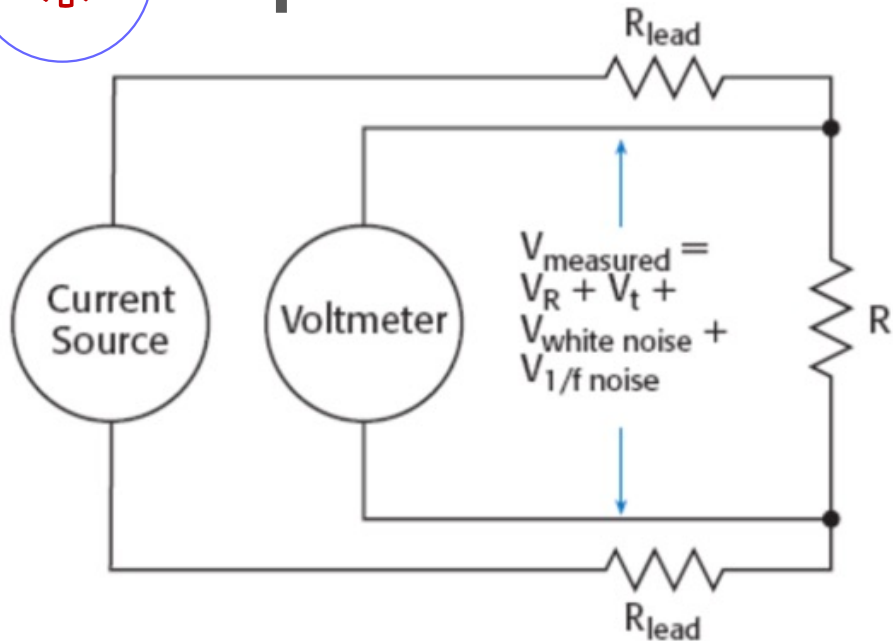
$$V_G = 0 \quad \frac{R_2}{R_1} = \frac{R_x}{R_3}$$

$$R_x = R_3 \frac{R_2}{R_1}$$

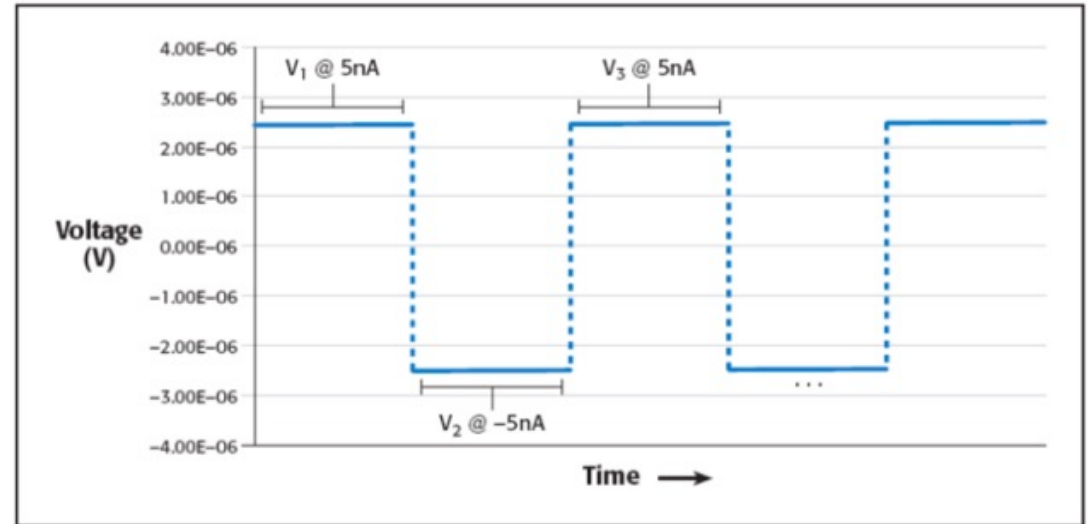
Wheatstone bridge for small resistance



Experimental Methods



Delta Mode



Wires generate spurious DC Voltages

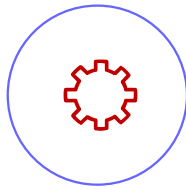
- Thermoelectric(thermal gradients) 1/f noise
- Galvanic (oxidation) 1/f noise
- RF interference and rectification in contacts

$$V_M = IR + V_{\text{offset}}$$

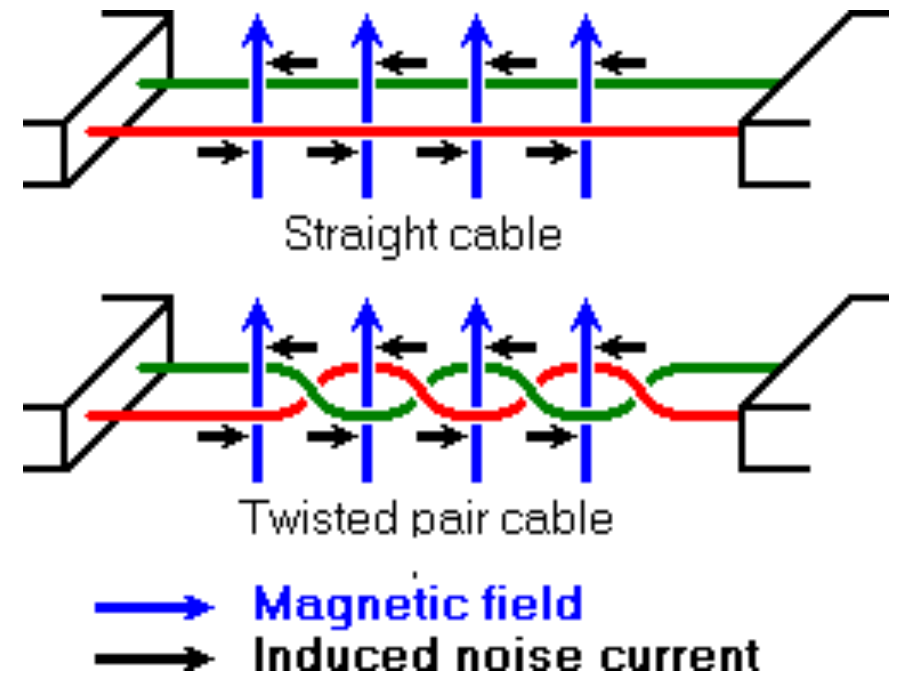
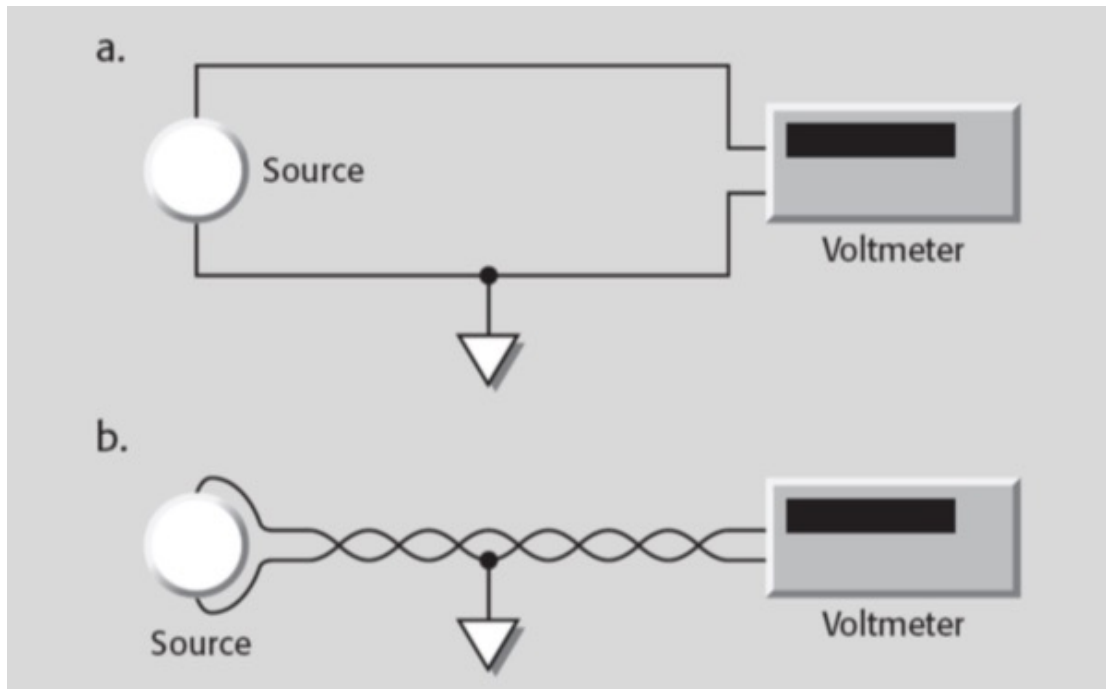
Noise sources

$$V_{M+} = IR + V_{\text{offset}} \quad V_{M-} = -IR + V_{\text{offset}}$$

$$V_M = \frac{V_{M+} - V_{M-}}{2} = IR$$

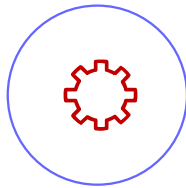


Experimental Methods

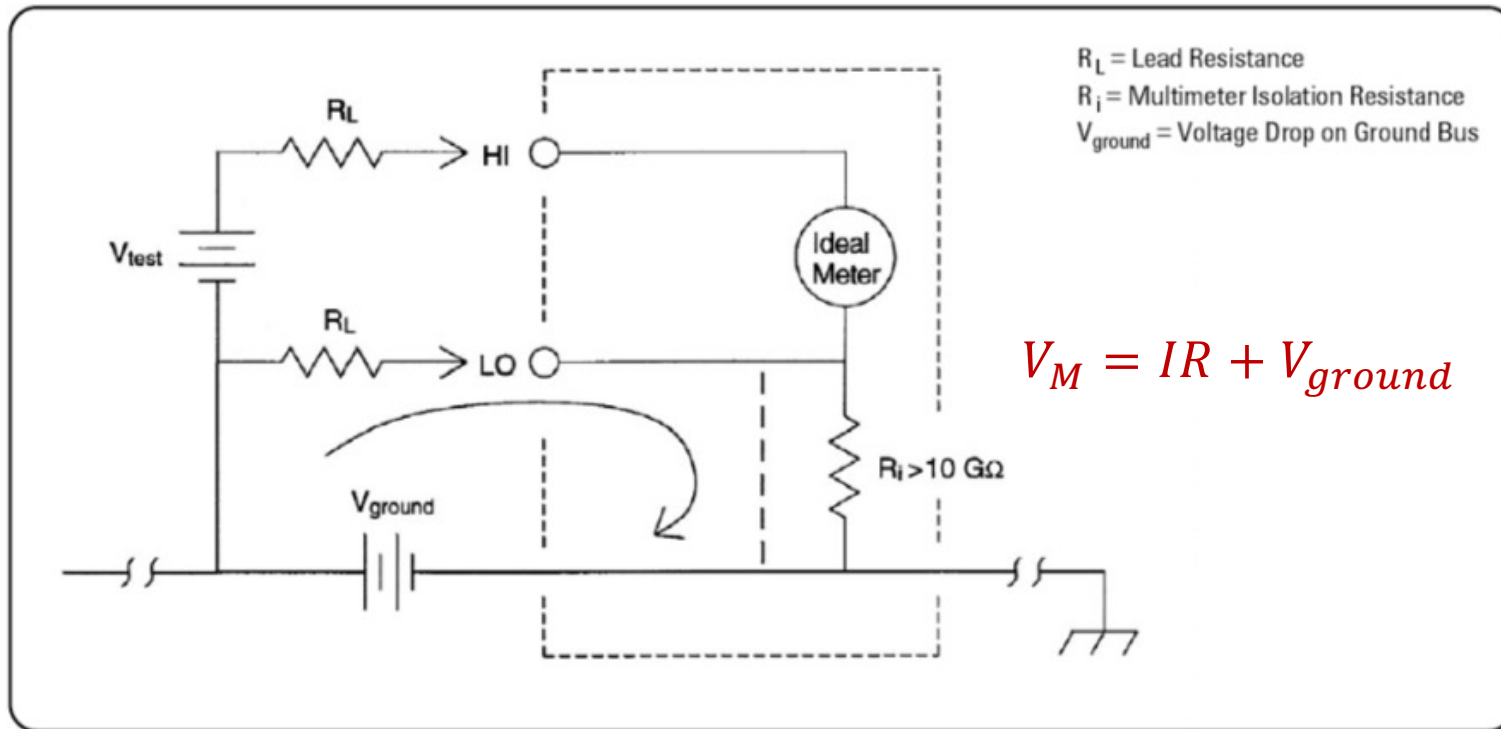


Minimizing interference from magnetic fields

Electrical Transport



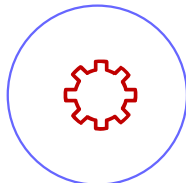
Experimental Methods



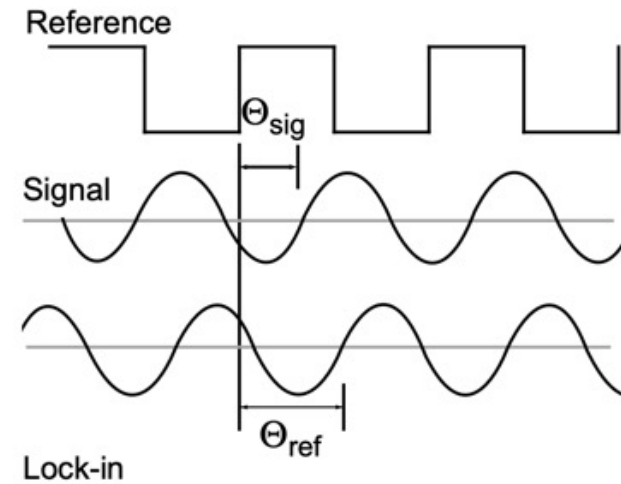
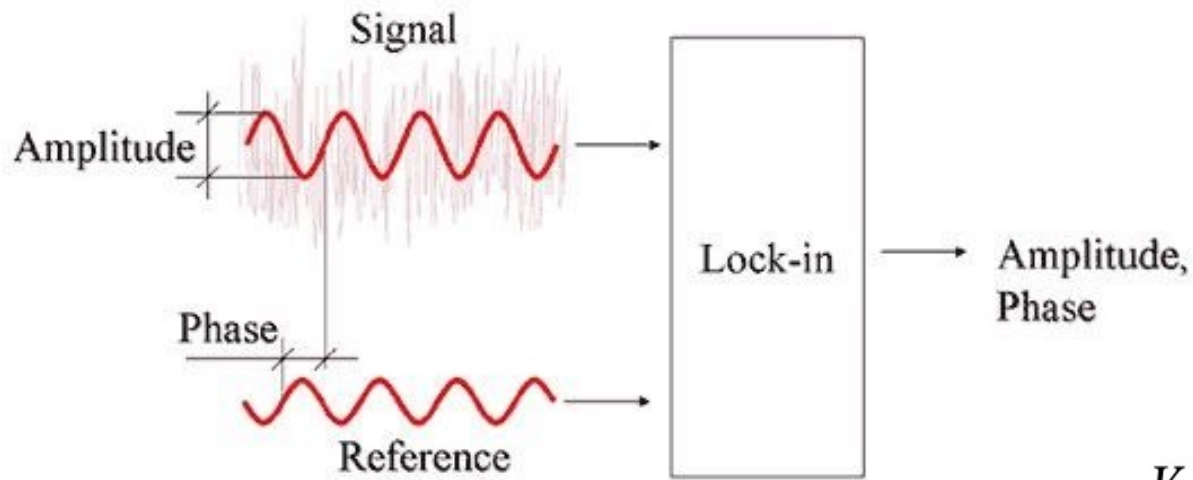
Devices grounded in different points acquire potential difference which contributes to the measured signal.

Ground Loop

Electrical Transport



Experimental Methods



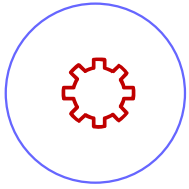
$$V_{MI} = V_I V_R \sin(\omega_R t + \theta_I) \sin(\omega_R t + \theta_R),$$
$$V_{MI} = \frac{1}{2} V_I V_R \cos(\theta_R - \theta_I) + \frac{1}{2} V_I V_R \sin(2\omega_R t + \theta_R + \theta_I).$$

Low pass filter

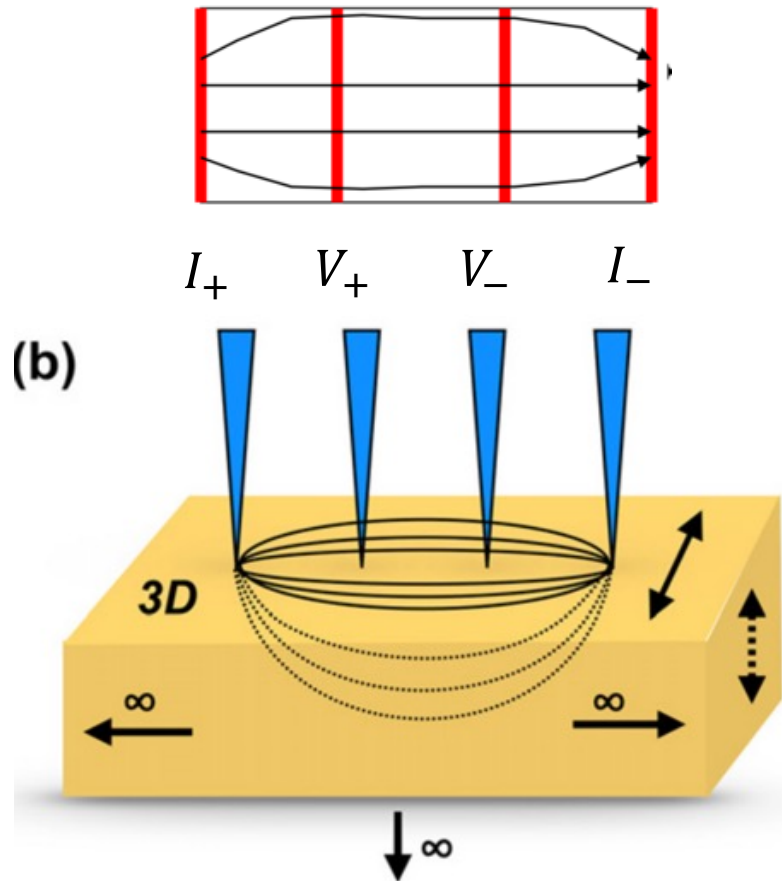
$$V_{MI+FILT} = \frac{1}{2} V_I V_R \cos(\theta_R - \theta_I)$$

Lockin method for low resistances

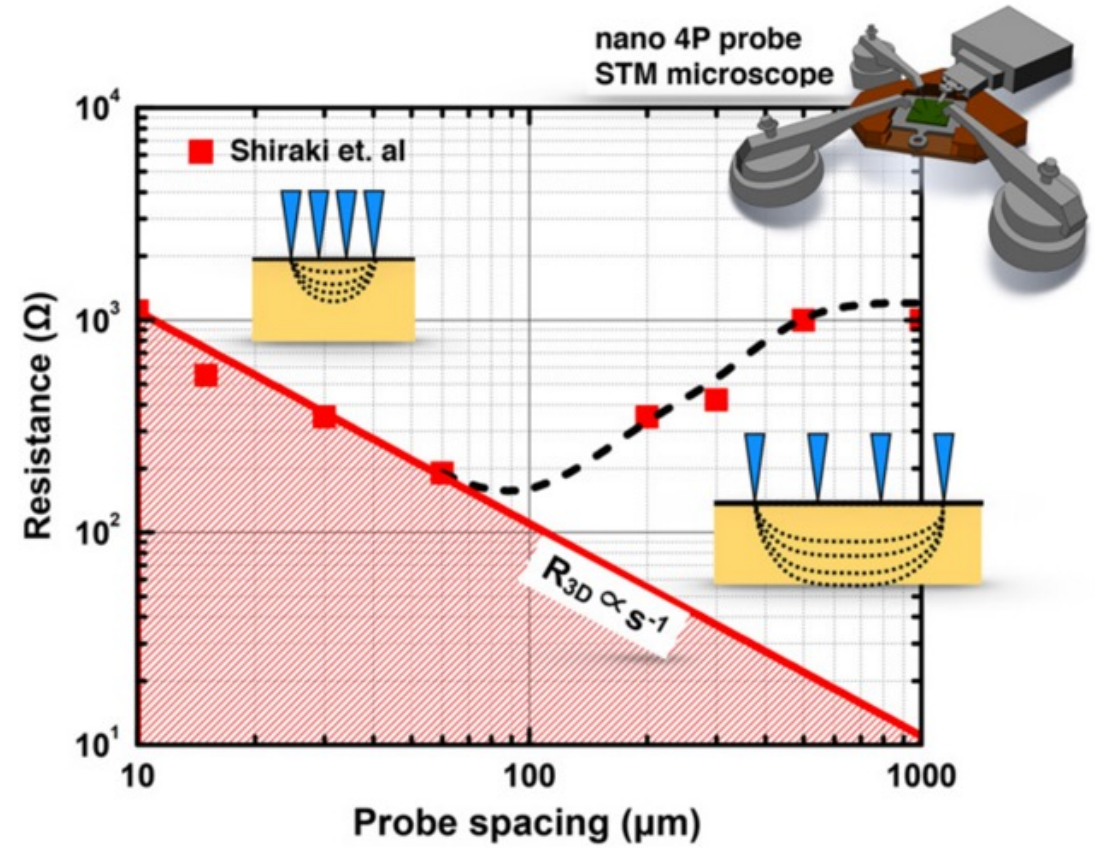
Electrical Transport



Experimental Methods

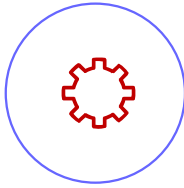


Sample shape



- “Ohmic contacts”
- Long and thin Bar

Electrical Transport



Experimental Methods

VOL. 13 No. 1

FEBRUARY 1958

Philips Research Reports

EDITED BY THE RESEARCH LABORATORY
OF N.V. PHILIPS' GLOEILAMPENFABRIEKEN, EINDHOVEN, NETHERLANDS

R 334

Philips Res. Repts 13, 1-9, 1958

A METHOD OF MEASURING SPECIFIC RESISTIVITY AND HALL EFFECT OF DISCS OF ARBITRARY SHAPE

by L. J. van der PAUW

537.723.1:53.081.7+538.632:083.9

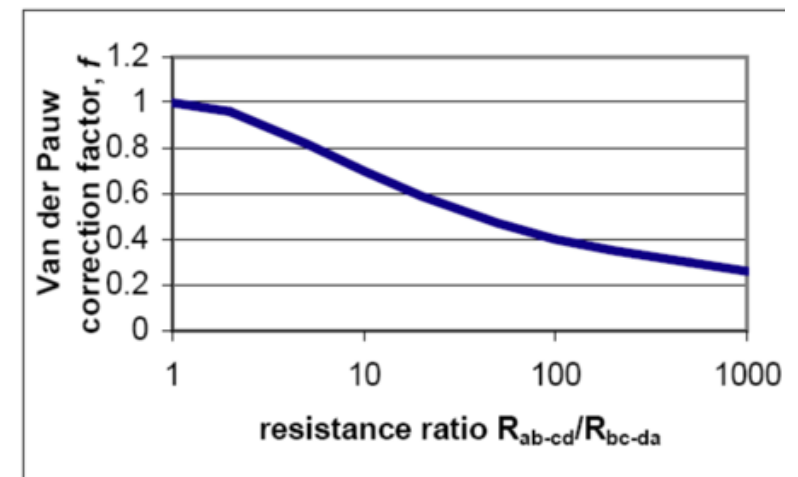
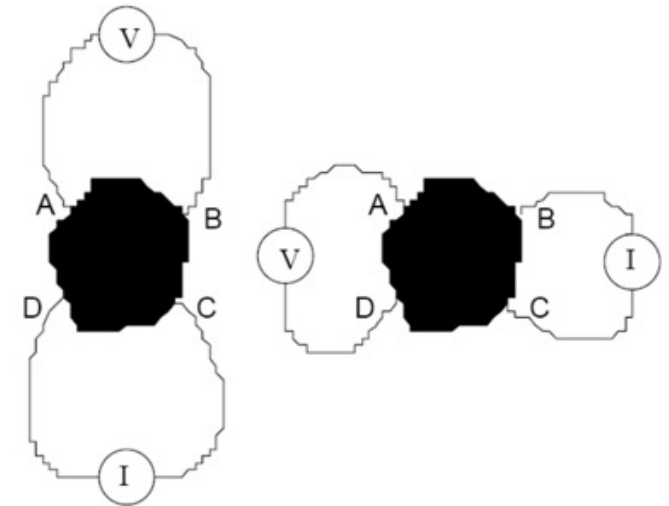
Summary

A method of measuring specific resistivity and Hall effect of flat samples of arbitrary shape is presented. The method is based upon a theorem which holds for a flat sample of arbitrary shape if the contacts are sufficiently small and located at the circumference of the sample. Furthermore, the sample must be singly connected, i.e., it should not have isolated holes.

Assumptions

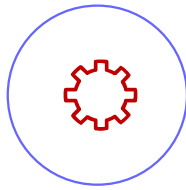
1. Homogeneous sample.
2. Isotropic sample.
3. Two-dimensional, thickness is unimportant.
4. Sample boundary sharply defined.

$$R_{sheet} = f \frac{\pi}{\ln 2} \frac{R_{AB-CD} + R_{AD-BC}}{2}$$



van der Pauw Method

Electrical Transport



Experimental Methods

JOURNAL OF APPLIED PHYSICS

VOLUME 42, NUMBER 7

JUNE 1971

Method for Measuring Electrical Resistivity of Anisotropic Materials

H. C. MONTGOMERY

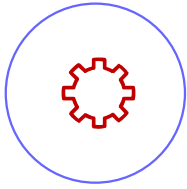
Bell Telephone Laboratories, Incorporated, Murray Hill, New Jersey 07974

(Received 30 November 1970)

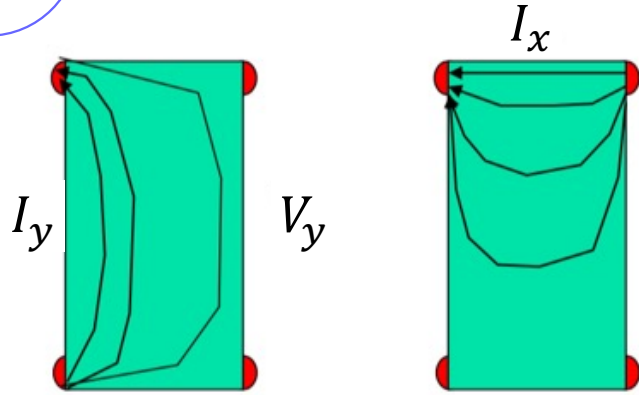
A rectangular prism with edges in principal crystal directions is prepared with electrodes on the corners of one face. Voltage-current ratios for opposite pairs of electrodes permit calculation of components of the resistivity tensor. The method can use small samples, and is best suited to materials describable by two or three tensor components. Examples are given of measurements of V_2O_5 -Cr and oriented amorphous graphite.

Montgomery technique

Electrical Transport

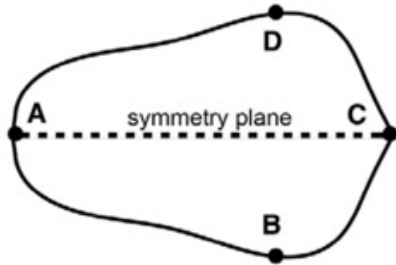


Experimental Methods

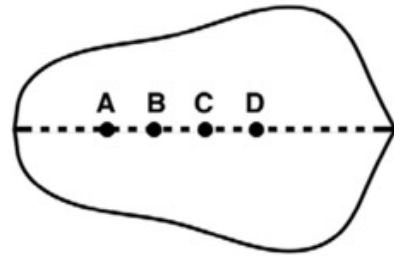


$$R_y = V_y / I_y$$

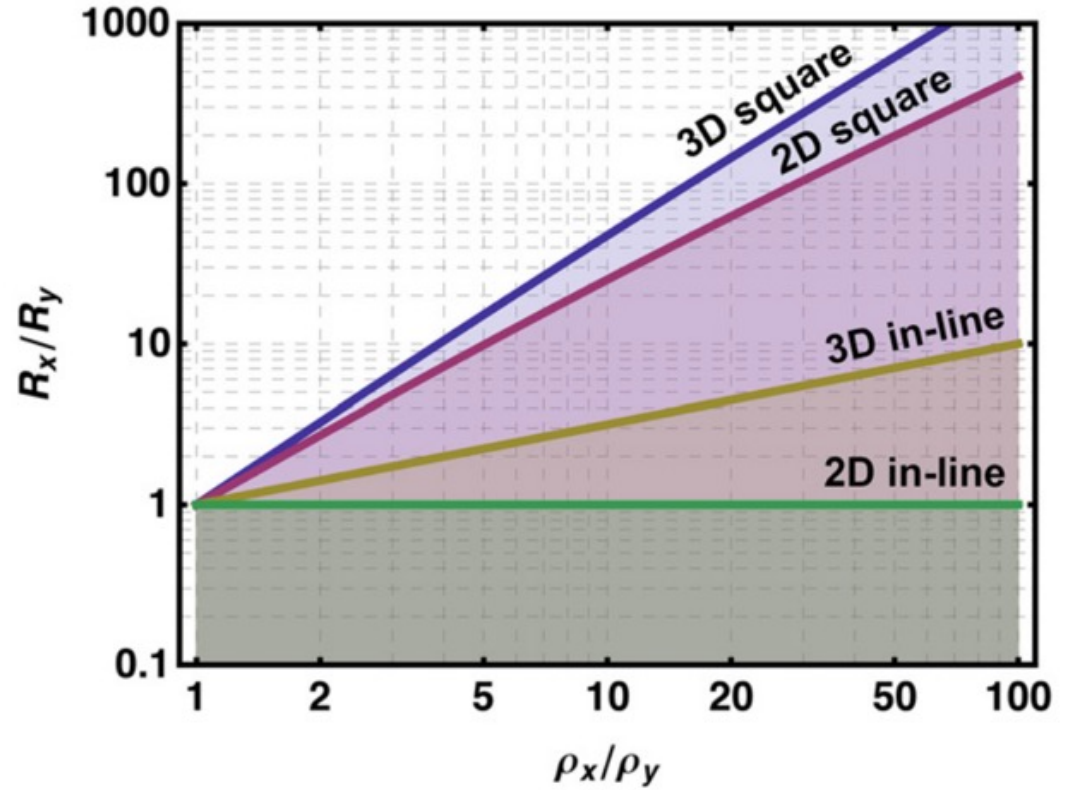
$$R_x = V_x / I_x$$



(b)

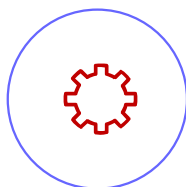


(c)



Montgomery technique

Electrical Transport



Experimental Methods

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[doi:10.1088/0953-8984/27/22/223201](https://doi.org/10.1088/0953-8984/27/22/223201)

Topical Review

The 100th anniversary of the four-point probe technique: the role of probe geometries in isotropic and anisotropic systems

I Miccoli^{1,2}, F Edler¹, H Pfnür¹ and C Tegenkamp¹

¹ Institut für Festkörperphysik, Leibniz Universität Hannover, Appelstrasse 2, D-30167 Hannover, Germany

² Dipartimento di Ingegneria dell'Innovazione, Università del Salento, Via Monteroni, I-73100 Lecce, Italy

E-mail: miccoli@fkp.uni-hannover.de

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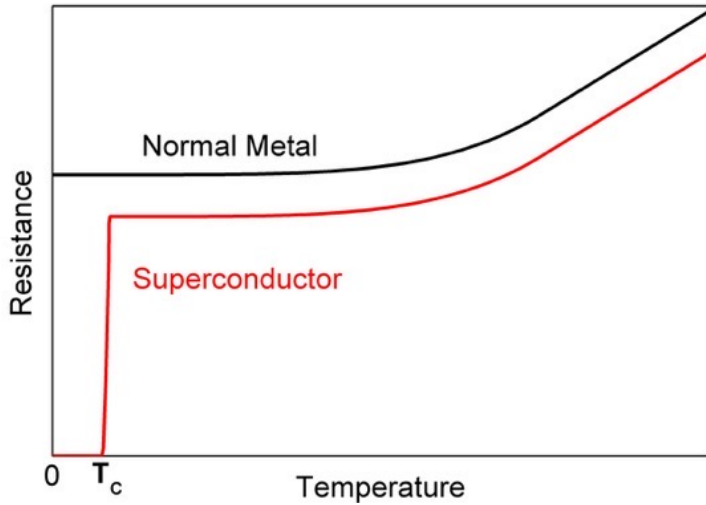
Electrical Transport



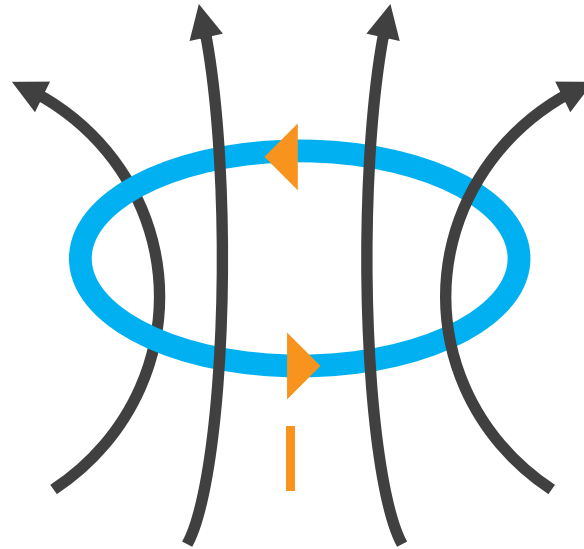
Summary



H. Kamerlingh Onnes

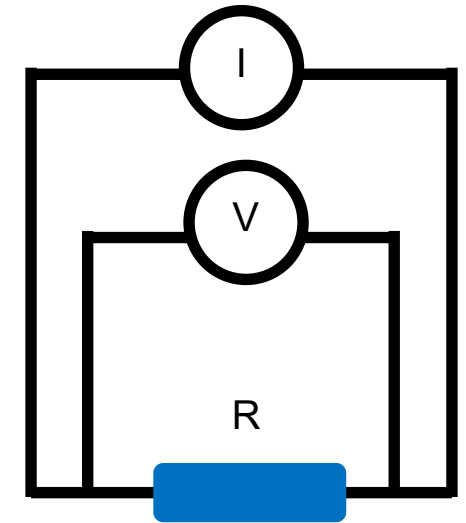


Discovered in 1911



Persistent Current

Application in superconducting magnet



Kelvin four-probe method

Chapter 1 Zero Resistance